A multispecies simulation for the management of the southern Gulf of St. Lawrence cod stock

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## Introduction

Cod (Gadus morø̌ua L.) have been fished in the Gulf of St. Lawrence for more than a century during the ice-free summer months. Prior to the mid-forties the fishery was primarily by baited hook or jigger, and it was not until otter trawls were first introduced by canadian fishermen that any significant changes took place in this fishery. The introduction of foreign otter trawls in the mid-fifties had a major effect on the fishery.

This cod stock, delineated in three tagging studies has been shown to occupy only ICNAF Division 4 T and Subdivision 4 Vn (Mccracken 1959; Martin and Kohler 1964; Kohler MS 1975). There are two main areas where the fish appear to congregate and where the fishery on them is concentrated: first, the Magdalen Shallows between the Magdalen Islands and the GaspéBay Chaleur; and second, the edge of the Laurentian Channel off the northeast coast of cape Breton. The annual migratory pattern is from the Magdalen Shallows in the fall to the area of dense winter concentration in the so-called sydney bight. In May, following "break-up", they again migrate to spawn in the highly productive shallows of the southern Gulf (Palohiemo and Kohler 1968). This stock supports two fisheries, the summer fishery in the southern Gulf of st. Lawrence and the winter fishery off Cape Breton. Traditionally, increases in fishing effort have been associated with increased foreign interest in the winter fishery.

Between 1936 and 1953 the average catch from this fishery was approximately $33,000 \mathrm{M} . \mathrm{T} ., \mathrm{a}$ figure which fishermen at the time thought was optimal for a sustained fishery. The fishery would probably have continued at this level if it had not been for the onset of the epzootic disease (Sinderman 1958).

The epizootic disease had catastrophic effects on the Gulf of St. Lawrence ecosystem by virtually decimating the . entire pelagic fish community. From a scientific point of view it was rather opportune since this violent perturbation allowed for a wide fluctuation in the stock-dependent variables controlling the cod production system. Thus, as in good experimental design variations in the independent variables became great enough that significant changes in the dependent variables could be noted.

Furthermore, the "die-off" of the pelagic biomass facilitate the growth of cod Kohler (1964), improved recruitment (Lett and Doubleday 1976 ) and generally led to an increase in the exploitable cod biomass. During the period between 1954 and 1957 there were four year-classes of aged 3 fish in excess of $10^{8}$. These sort of changes have also been noted in the North Sea where the increase in cod biomass is attributable to the decline in the pelagic biomass (Jones MS 1976).

In the late fifties the pelagic biomass in the Gulf of St. Lawrence began to recover with two large, 1958-59, herring (Clupea harengus harengus) year-classes being produced in conjunction with the 1959 year-class of mackerel. As the pelagic biomass increased the $3+$ cod biomass declined rapidly from a high of $560,000 \mathrm{M} . \mathrm{T}$. in 1955 to a low of $156,000 \mathrm{M} . \mathrm{T}$. by 1967; in part due to a substantial increase in fishing effort. During this period the average catch of the Southern Gulf stock was 78,000 M.T. with the peak catch in 1956 being llo,000 M.T.

However, a preliminary analysis of the data would show that the management of this stock is only partially reliant on the manipulation of fishing effort. Indeed, the calculation of fishing mortality between 1960 and 1975 indicates that the exploitation rate is much lower than has been experienced by other cod stocks fished in a sustainable manner. Thus the present critically low level of stock biomass is probably more the result of interactions with other fish stocks than the effects of so-called single-species-model exploitation.

This paper attempts to interpret the effects of multispecies interaction in the light of the internal dynamics of the cod stock as it relates to its management. Two previous papers (Lett et. al. 1975 and Lett and Doubleday 1976) have set the framework for this further attempt. It is anticipated that some earlier confusion related to the bioenergetics can be clarified and the very important relationships between population energetics and stock management will be elucidated.

## The Basic Data for Assessment

Catch-at-age data
A detailed discussion of the basic data between 1960 and 1970 has previousiy been presented by Halliday (1972), however it is probably worthwhile to present a brief summary. Six categories of landings are considered: otter trawl landings in the periods January-April, May-August, and September-December, seine, line, and gillnet landings. Biological sampling for length and age composition of landings in these categories in
the $1960-76$ period are good only from the Magdalen Shallows "summer trawl fishery". It was considered more appropriate to treat the winter Sydney Bight fishery separately despite poor sampling by all countries. Coverage of this fishery since 1970 has vastly improved especially since the fishery is now largely Canadian. Danish and Scottish seine landings were treated separately when samples were available and combined with otter trawl landings when there were no seine samples. While seine landings differed slightly from trawl caught fish, being smaller and younger they formed such a small part of the total that the error introduced by combining seine with trawl landings is small, but presently this is not the case (Table 1). However, gillnet and line landings could not be combined with trawl landings since the selection pattern in this fishery differs markedly from that for otter trawls. When there were no length frequency samples from line or gillnet landings in a particular year, those of the preceeding and subsequent years were combined and some 1971 samples were applied in this way to the inmediately proceeding years. Since 1970, the sampling of all fisheries has been thorough and no interpolating from other years was necessary (Table 1).

Catch-at-age data between 1950 and 1960 should be treated with some caution since sampling information is only available for the winter trawl fishery for the entire period (Palohiemo and Kohler 1968). Long and handiines and some gillnets made up a substantial proportion of the fishery during this period in addition to an inshore otter trawl fleet of small vessels. In years when samples were available for these gear types they were weighted into the overall catch-at-age frequency accordingly, but in years when samples were lacking an average catch-at-age frequency for that gear type was used. A substantial amount of discarding, from 1950 until the mesh regulations were strictly enforced in 1957 , was practised especially of $3-$ and $4-y e a r$ old fish. No detailed sampling of the discard is available to weight up the samples, but calculations show that the average estimation of year-class size during this period could not be underestimated by more than 10\%. Catch-at-age data for the period from 1950 to 1976 is presented in Table 2 .

Effort Data

The previous discussion indicates that the Gulf of St. Lawrence cod fishery is indeed diverse and between the period 1950-1976 the gear types, fishing power and gear efficiency changed dramatically. The only gear type for which effort data is consistently available is the 26-50 ton otter trawl fishery. Therefore this gear type has been used as the standard for the period. One aspect that detracts from
from its usefulress, upon first inspection, is that only ~ $7 \%$ of total catch is made by it as compared with $75 \%$ in early 50's. However, the correlation between the catch per unit effort (C.U.E.) of 26-50 ton vessels and 5l-100 ton vessels from 1962 to the present is very good suggesting that the catch rate in this fishery still roflects the catch rates in the overall fishery.

Changes in efficiency
The efficiency and fishing power of the Gulf of $S t$. Lawrence fleet most certainly has changed since the otter trawl fishery first began in l947. The progressive build up of larger trawlers and the decline in prominence of the gillnet and longline fishery are only a few of these changes. To analyse for an alteration in gear efficiency a trend was sought between fishing mortality per unit effort (F.U.E.) and time. The fishing mortality values were those generated by virtual population analysis. It was noted that $F$. U.E. increased exponentially with time suggesting that efficiency was increasing at a constant rate. A relationship of this sort had previously been hypothesized (Halliday and Doubleday 1976) for Scotian Shelf stocks in general. Their conclusion was arrived at by an indirect method, resulting from an iterative fitting of general production models.

The relationship hypothesis for analysis was
(I) F.U.E. $=\beta_{O} \operatorname{EXP}\left[\beta_{I} \Delta t\right]$

The reduction in the total sums of squares after fitting the mean due to exponential of $\Delta t$ was $39 \%$ while $\beta_{1}$ was equal to 0.0313 . This would suggest then that effort for this fishery was increasing at a rate of $3.13 \%$ per year since at least after 1957 when the proper mesh selections were enforced. Effort values were then adjusted by multiplying them by $\operatorname{EXP}[0.0313 \Delta t]$ where 1950 was considered year zero.

In 1976 the southern Gulf of St. Lawrence was closed to fishing by vessels $>100^{\prime}$. In addition, the number of large vessels fishing in 4 Vn was substantially reduced. This probably ended the continual gain in efficiency with the virtual closing of the 4 Vn fishery in 1977 the efficiency is probably equivalent to that in the early 60's. Many of the small inshore vessels fishing mow were built during this period, thus it would seem the fishery has reverted back to its nature in former times.

| YEAR | EFFORT/TRIPS | CATCH/M.T. | C.U.E. |
| :---: | :---: | :---: | :---: |
| 1950 | 3289 | 44023 | 13.38 |
| 1951 | 2771 | 34827 | 12.57 |
| 1952 | 3516 | 41956 | 11.93 |
| 1953 | 6572 | 58911 | 8.96 |
| 1954 | 6879 | 63901 | 9.29 |
| 1955 | 7592 | 65227 | 8.59 |
| 1956 | 10004 | 104469 | 10.44 |
| 1957 | 8917 | 89131 | 10.00 |
| 1958 | 10804 | 86582 | 8.01 |
| 1959 | 7706 | 70720 | 9.18 |
| 1960 | 12846 | 66013 | 5.14 |
| 1961 | 9144 | 65583 | 7.17 |
| 1962 | 8585 | 66664 | 7.77 |
| 1963 | 9846 | 70202 | 7.13 |
| 1964 | 9638 | 60547 | 6.28 |
| 1965 | 10786 | 63027 | 5.84 |
| 1966 | 15039 | 54851 | 3.65 |
| 1967 | 9562 | 41314 | 4.32 |
| 1968 | 7146 | 46551 | 6.51 |
| 1969 | 6438 | 47512 | 7.38 |
| 1970 | 8874 | 64459 | 7.26 |
| 1971 | 11305 | 56375 | 4.99 |
| 1972 | 13598 | 67733 | 4.98 |
| 1973 | 13446 | 50635 | 3.77 |
| 1974 | 19340 | 48746 | 2.52 |
| 1975 | 13741 | 39085 | 2.84 |
| 1976 | No data |  |  |
| 1977 | 4221 | 21096 | 4.99 |

Gear selection
Because of the diverse nature of this fishery and its affinity for constant change a valid sequential population analysis could not be preformed until something was known about selection, so that proper starting fishing mortality (F) values can be determined. Virtual population estimates will always vary in the proper direction when incorrect starting values are used, however these values cannot be considered correct until the selection is known. Since 1957 the $41 / 2^{\prime \prime}$ otter trawl mesh standard has been strictly enforced although the author is not naive enough to believe the violations of this standard would not lead to some biases within the data. The only selection experiments were carried out on otter trawl selection. The selection ogive was the cumulative distribution function of a normally distributed random variate (Fig. l) with mean 40 cm and standard deviation 7.5 cm derived from the data in Holden [ed.] (1971).
(2)

$$
\partial_{a}=\frac{1}{7.5 \sqrt{2 \pi 0}}
$$

$\operatorname{EXP}(-[(x-40) \times 7.5])^{2} d x$

In the case of long and handline selection and gillnet selection it was necessary to turn to the commercial catch sampling data. The strong 1959 year-class was chosen to follow through between ages 4 and 14 so the year-class effects would not confound the analysis. The fraction of the total catch attributable to each 30 cm length class was accumulated over the years between 1960 and 1974 as the Year-class grew in length and passed through the fishery. These accumulated fractions gave a selection curve but were confounded with the effects of the abundance at given lengths.

For this reason a relationship was found between the cohort numbers at age and the average length of the cohort as it grew older. A predictive equation was developed and abundance levels for each 3 cm length grouping were estimated. By dividing these estimates into the accumulated percentages a more unbiased estimate of selection could be determined assumingly with the effects of varying abundance removed. Polynomials were fit to these relationships of the form
(3) $\cdot \partial_{a}=\beta_{o} \operatorname{EXP}\left[\beta_{1} L_{a}-\beta_{2} L_{a}{ }^{2}\right]$
and the maximum of the curve was given as selection of one (Figure 1). Selection in the otter trawl fishery begins at approximately 22 cm while in the longline fishery selection begins at 37 cm and 49 cm for the gillnets. Full selection in the otter trawl fishery occurs at $61 \mathrm{~cm}, 73$ in in the long and handline and 86 cm in the gillnet. Danish seine selection is assumed to be the same as otter trawl selection.

It is rather peculiar that the selection in the long and handline fishery falls away so symetrically, however this response has been noted for other line fisheries. It would seem that the cod no longer prefer the bait in addition to the fact that the hook size may become inefficient. It is doubtful that they are not merely available to the gear since the division between size groups of fish seems to be more related to maturity. Furthermore, research surveys indicate that cod over 73 cm are available in areas of longline fishing.

These three selection curves were combined such that an overall selection for each year since 1960 could be determined for the fishery. Weighting factors were calculated for each age group and combined based on the overall catch in numbers of that age group within the gear type; the mean length of the age group dictating the selection. The results of these calculations are shown in Table 3.

Sequential population analysis
Cohort analysis (Pope 1972) was utilized to determine the numbers at age. Starting values were determined using an iterative process. First a guess was made for starting $F$ values in 1975 and this was distributed over age according to the selection factors in that year. The starting for the terminal ages in the different years was 0.2. Natural mortality (M) was held constant at 0.2 for all age groups. A preliminary study using Palohiemo's method indicated this to be correct for ages 3 to 14 when the $C . U . E$. was divided by the selection factors. However, this is not to say natural mortality does not vary with age, it is merely an average value when the geometric mean regression is used for bivariate normal data (Ricker 1973).

Estimates from cohort analysis improve as $F$ values accumulate, thus after the initial run the average $F$ was determined for fully recruit age class and $F$ values for terminal years were determined by multiplying these average f's by the appropriate selection factor. The $F$ value in 1975 was determined from a plot of fishing mortality vs effective effort. The analyais was again run, and the same procedure was followed with the exception being that the total average $F$ for ages 3 to 15 was now correlated with effective effort until the deviation of 1974 plus 1975 from the G.M. regression line was minimized (Fig. 2).. Since no selection factors were available prior to 1960 an average value of 0.28 was used in the terminal years.

The correlation between $\mathrm{F}_{3-16}$ and effective effort is quite good and does indicate that management of fishing effort can have substantial impact on the resultant mortality rates within the cod stock. The lack of trends in the residual would indicate errors are occurring randomly and there are no between year effects in natural mortality although nothing can be said for this relationship about age effects. The correlation of effort $x$ selection against $F$ does show a trend in the residual and this may be attributed to age specific natural mortality. Numbers at age and $F$ values are shown in tables 4 and 5.

The relationship in Fig. 2 supports the idea of an increase in efficiency up until 1975. However, it does not indicate that the numbers at age are completely correct, especially in most recent years. The check on this relationship, the numbers of $3+$ fish from VPA in year $t+1$ were plotted against the catch of $2+$ fish from the Gulf surveys in year $t$. The reason for the 1 year lag is that the standard Gulf cruise occurs in

October when the fishing is almost over and the birthdate for virtual population analysis is January lst.

The abundance levels were taken from fixed stations in the Shediac Valley, Bay of Chaleur area. This is the area of highest cod abundance according to the stratified random survey over the entire Gulf of St. Lawrence (Fig. 4). Two facts are important when interpreting this relationship. First the correlation is excellent indicating that the virtual population analysis corresponds very well with catches in the survey expecially since the data is not a time series. Therefore, it is very likely that the numbers at age from virtual population analysis actually are close to the real numbers at age. The second aspect is that this relationship does not go through the origin suggesting that perhaps numbers at age are in fact over-estimated. However, since ages 2, 3 and some of 4 are not fully recruited to the research gear, the CUE is an underestimate of the real CUE if all fish were available.

The CUE from the Gulf surveys are variable from year to year. Therefore, these numbers are smoothed using a 3 year running average since it is really the average of 2,3 and 4 year olds that make up the bulk of the index.

| YEAR | CUE 2+ cod <br> Gulf survey year $t$ | CUE 3 year <br> average | Numbers of $3+$ <br> from VPA year $t+1$ |
| ---: | :---: | :---: | :---: |
| 1962 | 189 | 170 | 266,945 |
| 63 | 133 | 156 | 235,666 |
| 64 | 145 | 125 | 208,242 |
| 195 |  |  |  |
| 66 | 95 | 112 | 192,111 |
| 67 | 95 | 161 | 231,893 |
| 68 | 291 | 181 | 261,517 |
| 69 | 155 | 181 | 245,352 |
| 1970 | 95 | 132 | 228,406 |
| 71 | 144 | 96 | 227,120 |
| 72 | 48 | 92 | 189,026 |
| 73 | 84 | 62 | 161,273 |
| 74 | 52 | 58 | 161,729 |
| 1975 | 37 | 61 | 149,755 |
| 76 | 94 | 87 | 174,837 |
| 77 | 128 | 149 | 202,569 |

Using the smoothed value for 1977 gives a predicted numbers at age in 1978 of approximately $2.6 \times 10^{8} 3+$. The catch projection from 1977 using the catches generated in that year gives a total of $1.6 \times 10^{8} 4+$ cod in 1978. Thus by subtraction the estimated 1975 year class size is $1.1 \times 10^{8}$ in 1978 .

Juvenile surveys and the prediction of year class size.
Previously a correlation was found by Hare and Kohler (1975) between the logarithm of the CUE of juveniles and year class size as estimated from virtual population analysis. Further analysis of this data indicates that the transformation is unwarranted, thus the geometric mean is used here. Since the juvenile surveys in former years did not cover the entire Gulf of St. Lawrence, and were conducted with different mesh and vessel sizes, the two surveys needed to be intercalibrated.

The correlation between the catch per tow of the old and new surveys was almost perfect for 1971 to 1973 . The values from the old surveys between 1957 and 1970 were now corrected to be equivalent to the new random stratified surveys.

| YEAR CLASS | CUE AGE 2 | VPA ESTIMATED <br> AT AGE $3 \times 10^{3}$ |
| ---: | ---: | ---: |
| 1957 | 17.32 | 134,847 |
| 58 | 3.10 | 46,119 |
| 59 | 3.53 | 60,134 |
| 1960 |  |  |
| 61 | 3.68 | 41,739 |
| 62 | 4.86 | 61,261 |
| 63 | 3.63 | 52,501 |
| 64 | 4.58 | 61,429 |
|  | 16.87 | 107,042 |
| 1965 | 6.92 | 95,111 |
| 66 | 7.53 | 56,944 |
| 67 | 2.04 | 50,480 |
| 68 | 6.96 | 74,245 |
| 69 | 0.62 | 23,460 |
| 1970 | 3.63 | 45,780 |
| 71 | 6.98 | 69,137 |
| 72 | 2.54 | 42,135 |
| 73 | 8.90 | 80,814 |
| 74 | 9.41 | 83,915 |
| 1975 | 26.42 | 187,363 |

The correlation between the numbers at age 3 from VPA and the catch of age 2 cod of the same year class from the juvenile surveys, was indeed high ( $r=0.90$ ). The equation for the geometric regression was as follows:
(4) $\quad N_{3}=6081.58$ C.U.E. $2+26687$

## 11.

Because of the contagious nature in which cod are distributed and the fact there is a segregation of small cod from larger cod, it is quite possible to overestimate the catch per unit of effort for young cod when they are abundant. The survey has not been stratified, or randomized for the matter, for the distribution of different age classes of cod. These young fish are mainly concentrated around Miramichi Bay (Fig. 4) and spread our from there in diminishing numbers. In 1977 large catches of small fish occurred throughout this region.

The basic data for the assessment presented here is now complete, but very little of the actual biology of these relationships has been discussed. Before further analysis is performed, a detailed biological analysis will be presented, and a simulation built for further prediction.

## The Biological Background to the Assessment

Density Dependent Growth
The instantaneous growth rate of cod ages 2-15 was defined as $G=\frac{d w}{d t w}$ and calculated from weight at age data from commercial catch sampling between 1950 and 1975 (Table 5). These samples were all taken between January and April when the cod are not growing. The instantaneous growth rate can be calculated by the natural logarithm of the ratio of weights in successive years (Ricker 1958).

Lett and Doubleday (1976) have previously shown that the growth rate of cod between ages 5 and 8 in the Gulf of St. Lawrence is inversely related to the biomass, and that the biomass indeed reflects the density since no changes in catchability have been noted during the period. However, since this is an average rate it is difficult to apply it to the overall stock. According to Kerr (1974) the instantaneous growth fishes should be an inverse power function of their weight. In theory this is fine boworer one wonders to what degree the fit of such a relationship is due to the auto correlation of the independent and dependent variables. Laboratory experiments have shown that the basal metabolic rate of fish drops with size (Beamish et. al. 1975) suggesting that this relationship is indeed correct; thus it would seem appropriate to linearize the data using a double logarithríc transformation for hypothesis testing.

Another variable, which does not vary in a continuous manner overtime, are the accumulation of events which occurred during the epizootic disease in the Gulf of St. Lawrence (Sinderman 1958). During the period from 1945 to 1958 the biomasses of mackerel and herring were almost totally decimated. The disease which started gradually and caused catastrophic mortalities near its termination may be related to higher than average water temperature which prevailed during this time. The growth rate of cod was increased since they were eating diseased herring which could easily be captured. Furthermore, more eneray was possibly being transferred directly into the

This would increase the carrying capacity of the benthos, and the number of available food items for young and old cod alike. This situation in the Gulf of st. Lawrence is similar to that noted in the North Sea where the pelagic biomass is now at a very low level because of over-exploitation, but substantial increases have been noted in the cod biomass. Jones (MS 1976) has presented a preliminary investigation of possible energy flows in the North sea system which elucidate the partitioning of energy such that the measured changes could occur.

Palohiemo and Dickie (1966) suggest the metabolic exponent is constant while the proportionality constant varies to environmental condition. Farmer et. al. (1977) found this was not true for the growth of sea lamprey since both the exponent and proportionality constants were acted on by environmental variables. For this reason the following form of equation is put forward to describe the growth of cod:

$$
\begin{equation*}
\frac{\mathrm{d} w}{\mathrm{dtw}}=\beta_{0} \cdot B^{-\gamma_{1}} \cdot W^{-\gamma_{2}} \cdot B^{-} \tag{6}
\end{equation*}
$$

where $B$ is the biomass of cod before the summer fishery begins and $W$ is the weight of cod in kg.

Multiple regression was used to determine parameter values and a dummy variable $D$ represents the collective effects of the epizootic disease on growth. The dummy variable is zero when there is no epizootic and one when it is occuring. The following adequately describes the instantaneous growth rate of cod:

$$
\begin{gathered}
\text { (7) } \log _{e} G=-0.0517 \log _{e} B \times \log _{e^{W}-0.2515 \log _{e^{B}}+} \\
0.1472 \log _{e} W \times D+1.88691
\end{gathered}
$$

| Variable | Coeff. | S.E. |
| :--- | :--- | :---: |
| $\log _{e}{ }^{B}$ | -0.2515 | 0.0922 |
| $\log _{e} B^{W} \times \log _{e} W$ | -0.0517 | 0.0050 |
| $\log _{e}^{W} \times D$ | 0.1471 | 0.0803 |

```
The coefficient of multiple determination ( \(R^{2}\) ) is 0.47 while \(F\) (significant at \(P<0.05\) ) for regression is
65.32 (F
The significant interaction between weight and the dummy variable indicates that when the epizootic is not occurring weight is more influential on growth rate. This would suggest that the epizootic infact increased the energy intake of cod which seems to be the case. Since the epizootic is not a "normal" event in the management of cod the most useful equation would be:
```

$$
\begin{equation*}
G=6.6000 B^{-0.2515} \times W^{-0.0517} \log _{e^{B}} \tag{8}
\end{equation*}
$$

As the weight of cod increases the growth rate declines rapidly (Fig. 6) with the growth rates of smaller fish being more effected by shifts in biomass than older fish. This would make density dependent growth in most fish stocks extremely hard to detect.

## Seasonal Growth of Cod

The seasonal growth pattern for cod is very difficult to determine from field data because of sampling errors and biomass. In addition, the collection of the data is expensive and probably substantially out weighs its value when the degree of uncertainty is considered. Thus monthly growth rates were determined by Waiwood (1978) for laboratory held fish at different temperatures and fed varying rations. It was found that growth rate followed appetite extremely well, and this was evident in a seasonal pattern. Using this data and considering the cumulative growth was calculated as a proportion of the maximum growth rate (Fig. 7). Growth rate declines during the initial part of the year and actually became negative in April to May prior to spawning. A maximum growth rate was reached in October with a further decline being evident in November and December. Thus, by using this data, it would be possible to calculate monthly catches when something is known about the seasonality of the fishery.

Bensity dependent $\tau_{1}$ growth
The occurrence of density-dependent growth during the first year of life in the Gulf of St. Lawrence cod stock was investigated using the back calculation of 2500 otoliths taken from commercial sample surveys for the years 1960-1975. For each year, 150 otoliths covering all available age groups were read according to the established methods of Kohler (1964) and May (1967). The
left otolith from each fish was broken across the sulcus, both halves were smoothed with emery paper when necessary, placed into a plasticene substrate, covered with alcohol and examined at $25 \times$ magnification under a binocular microscope. The interface between the outside edge of the opaque band and the inside edge of the hyaline zone was taken to be an annulus. The distances between the focus and each respective annulus were measured with the aid of an ocular micrometer in a radius perpendicular to the otoliths longitudinal axis. These distances were tabulated with the fishes length; values for crystallized or unreadable otoliths were not used. The regression between fish length $(L)$ and otolith radius ( $R_{0}$ ) was $L=0.628 R_{0}^{1.227}$ with an $R^{2}$ of 0.73 . According to age and year of capture, the otolith measurements for each fish were sorted into year-classes. The sample sizes ranged from 32 for 1950 year-class to 183 for 1964 and 27 for 1972. The mean length in centimeters for each year of growth for all year classes was tabulated.

Density-dependent $7_{1}$ growth has been shown to exist for clupeids (Marr 1960, Iles 1968, Lett and Kohler 1976) and for gadoids (Raitt 1939, Doubleday et al 1976). The information of the first annulus has been argued by Lett and Kohler (1976) as being a response to carrying capacity, environmental heterogeneity and predatory pressure. This predation is not a direct but secondary one, leading to the consumption of larvae and juveniles which are weakened by starvation (Jones, 1973). Both temperature and a holistic variable representing the change in the carrying capacity as a result of the epizootic disease should therefore significantly alter the information of $\tau_{1}$ length. The hypothesis was the $2_{7}$ length was a power function of yearclass size and the exponent could be altered by the logarithm of temperature. Again a dummy variable was used to represent the ep-zootic, 1 when it was occurring and 0 when not. The following equation described much of the variation in 27 length:
(9.) $\log _{e} Z_{1}=0.2999 \log _{e} N_{3}+0.27251 \log _{e} N_{3} \times D-$ $2.9395 \times D+0.02201 \log _{e} N_{3} \times \log _{e} T p+$ 4.71572

| Variable | Coeff. | S.E. |
| :--- | ---: | :--- |
| $\log _{e} N_{3}$ | -0.2999 | 0.0459 |
| $\log _{e} N_{3} \times D$ | 0.2725 | 0.0931 |
| D | -2.9395 | 1.0486 |
| $\log _{e} N_{3} \times T p$ | 0.02202 | 0.0132 |

The coefficient of multiple determination $\left(R^{2}\right)$ was 0.71 while

15.
$N_{3}$ is the numbers in a particular year class $\times 10^{-3}$ at age 3 , while $2_{1}$ is the length of the fish at the time of formation of the first annulus and Tp is the spring temperature at Grande Riviere on May 25.

As year class size increases, there is an exponential decline in $l_{1}$ length. The shape of this relationship agrees well with the exponential decline in $Z$, length for silver hake in response to year class size noted by Doubleday et al. (1976).

A more useful form of the equation when the epizootic is not occurring is:

$$
\begin{equation*}
I_{I}=5.907 \mathrm{~N}_{3}\left[0.5724+0.0222 \times \log _{e} T p\right] \tag{10}
\end{equation*}
$$

The yearly fluctuations in the first year of growth are most interesting. The variations could not be explained by either Lee's phenomenon or an increase in experimental error, in fact statistical confidence was highest for the first year growth measurements. The relationship between this crucial growth period and the ensuing recruiting stock size seemed to satisfactorily account for much of the variation. Concommitant with density dependent first year growth is a suggestion of growth compensation in the second and third years; where first year growth was low, second year growth was usually high, with the converse always being true.

The phenomenon of density dependent growth has been viewed as obvious by some and dubious by others cushing (MS 1976), but is certainly suggested by this study. This is probably because changes in the rate of accumulation of surplus energy are more manifested in fluctuations in gonadal rather than somatic weight in mature fish, making changes in body weight much harder to detect as fish get older.

## Shifts in maturity with length

Maturity for some time has been considered a fixed function of length. However, the recent works of Daan (1974) and DeVeen (1976) indicate that this biological trait is dynamic for cod and plaice. Shifts in the maturity ogive have also been noted
for Gulf of $S t$. Lawrence cod (Fig. 8) with the mean length of maturity dropping 13 cm since 1959. Small shifts in maturity can have an extreme impact on the total egg production of the population this it would seem that a trait as powerful as this one should have some biological significance. In addition, it is not intuitively obvious why maturity should shift with length.

It has been noted by Beverton (1959) that maturity. usually occurs at the inflection of the relationship og. growth over time. That is to say, when the rate at which fish are gaining weight over time begins to decline the fish reaches maturity. Therefore it would seem that the length at which maximal growth rate is achieved determines the onset of maturity.

It has been noted in mammalian populations that growth determires the age of maturity in addition to the size. Personal observation has shown that, rainbow trout fed a maximum diet will mature in the first year of life at a length far less than wild fish. For this reason, it was hypothesized that the growth rate of cod during the first year probably strongly influences the length at which they mature. Indeed, this does seem to be the relationship (Fig. 9). A mechanism such as this has strong homeostatic value in relation to maintaining population stability. A strong year-class grows more slowly in the first year of life and matures at a larger size. Thus the effect of this good year-class on the reproductive biomass does not as quickly as a small year-class. However, if a stock is collapsing and year-class size is beginning to diminish then these fish will mature much sooner than if the ogive were fixed, augmenting the size of the reproductive biomass quite dramatically. The effect of this relationship on the population stability and subsequent stock management will be discussed later.

## Cod Adult Stock Production and Egg Production

The mechanism by which the egg production of a fish stock is related to the production of the adult stock has been discussed by Lett (MS 1976), Lett and Kohler (1976), Lett et al (1975) and Tyler and Dunn (1976). Recently De Veen (1976) has presented data showing a continual increase of fecundity at length for sole either because of a decrease in stock or an increase in food or both. Bagenal (1973) has also not the same types of changes for North Sea plaice. Waiwood (1978) has presented data showing the egg production can be related to growth rate for cod.

The hypothesis being put forward in this paper is that fecundity is related to the food intake and the partioning of the proportion of surplus energy into gonad is reliant on the total available surplus energy. Mathematically this paradigm can be represented by the equation:
(11) $E=N \times(\Delta W)^{\gamma}$
where $E$ is the egg catch in the Gulf of St. Lawrence surveys per $100,000 \mathrm{~m}^{-3}$ of water, $N$ is the number of mature fish and $\Delta W$ is the weighted growth rate of the mature stock. The exponent, $\gamma$, is the rate at which surplus energy is being channeled to gonad in relation to the overall surplus energy represented by a change in weight. The distribution of eggs in the Gulf of St. Lawrence is shown in Figure 10.

Lett et al. (1976) have shown that temperature (Tp) influences the survival of eggs and influences the catches on the egg and larval cruises. In addition, it has been shown that temperature acts in a quadratic manner which agrees with the findings of Forrester and Alderdice (1966) and Bonnet (1939). There the following equation was fit using multiple regression to represent the catch of eggs during the time of peak spawning.
(12) $\log _{e} E / N=\beta_{1} \log _{e} \Delta W+\beta_{2} T p+\beta_{3} T^{2}+\beta_{o}$

| Parameter | $\frac{\text { Value }}{}$ | St.Error |
| :---: | :---: | :---: |
| $\beta_{1}$ | 1.2221 | 0.3640 |
| $\beta_{2}$ | 1.6769 | 1.1114 |
| $\beta_{3}$ | -0.1655 | 0.1071 |
| $\beta_{0}$ | 1.780 |  |

The reduction in the total sums of squares, after fitting the mean, due to regression was 77.3\%, with an $F=6.8\left(F^{l} 3.6 / 4.76\right)$. The equation can be rearranged to.
the
following form.

$$
\text { (13) } E=5.93 \times \operatorname{EXP}\left[1.677 T p-0.166 \mathrm{Tp}^{2}\right] \times N(\Delta W)^{1.222}
$$

where $T p$ is the mean sea surface temperature occurring on
the cruise. Although neither $B_{2}$ or $\beta_{3}$ are significant
the combined effects of the fitting of these two parameters led to an improvement to the overall fit of $9 \%$. Most of the variation in egg catch per mature individual is explainable by the growth rate, $69 \%$ or the production of surplus energy by individual fish (Fig. ll).

The existing dogma relates eggs production to the mature stock biomass and this is usually converted to eggs by the multipication of some fixed fecundity length relationship. Equation (13) shows that clearly for cod this is not the case. However, for a stock where $\Delta W$ did not change then there would be a linear relationship between biomass and egg production, but this has limited biological meaning. Twice (Lett et al. 1975), (Lett and Doubleday 1976) a dome shaped egg production curve has been presented as a function of biomass. It was hypothesised at that time that density dependent growth led to the production of this dome shaped curve. Equation (13) certainly supports this conclusion since according to equation (8) $\Delta W$ should decrease as $N$ increases and the rate at which egg produce declines with density depends on the exponent of $\Delta W$.

The production of Larvae

The survival of fish larvae has been a topic of particular concern to fisheries biologists for the past century. A number of notable papers have been produced relating the survival to environmental effects (Hjort l9l6, Hempel 1965, Postuma and Zijlstra 1974 and Cushing 1975) and the density dependent effects (Beverton and Holt 1957, Beverton 1962, Cushing and Harris 1973, Jones 1973, Cushing 1975) however, few papers consider the combined effects of the environment and density dependence presenting the results in a quantitative manner. Exceptions to this however are the works of Ware (1975), Lett et al. (1975) and Lett and Kohler (1976).

The model being developed in this paper incorporates the two effects and presents a quantitiative model. The normal assumption concerning the survival of fish is that:
(14) $\frac{d N}{d t}=B_{o} N$
or that the instantaneous growth rate is constant. Cushing (1975) and ware (1975) found this was not an adequate model for explaining both the mortality of fish larvae in addition
to older stages of fish. Cushing decided that instantaneous growth was indeed density dependent and reformulated the survivorship equation as:
(15) $\frac{d N}{d t}=B_{O} N^{2}$

Ware's (1975) sophistication of the problem hypothesizes that mortality is related to the growth rate an agreement which seems well supported by the data. Unfortunately, the data is not yet available on the growth of juvenile and larval cod so in this study it is proposed that the mortality rate responds to density.

It is assumed that the structure of the relationship between density is not known. A plot of the instantaneous mortality verses numbers over the period when larvae are available is an asymptotic relationship with population density such that:
(16) $\frac{d N}{d t N}=\beta_{1} \log _{e} N+\beta_{2}\left[\log _{e} N\right] x T p+\beta_{o}$

| Parameter | Value | S.E. |
| :--- | :--- | :--- |
| $\beta_{1}$ | $1.639 \times 10^{-2}$ | $2.470 \times 10^{-3}$ |
| $\beta_{2}$ | $1.751 \times 10^{-5}$ | $1.000 \times 10^{-5}$ |
| $\beta_{0}$ | -0.0485 |  |

where $T p$ is the annual monthly maximum temperature. The reduction in the total sums of squares, after fitting the mean, due to regression is $88.7 \%$ with an $F$ of $35.3\left(F_{2} l_{2}, 9 / 4.26\right)$. What the equation implies is that if the number of eggs is known and the temperature, the number of surviving larvae is predictable at a later date. Of all models considered equation l6 gave the best fit. This equation must be solved iteratively since there is no closed form for intergration. Thus the equation in the following form must be solved iteratively:
(17) $d N=\left[1.639 \times 10^{-2} \log _{e} N\left(1-1.0683 \times 10^{-3} T p^{2}\right)-0.0485\right] \times N_{0} \times d t$
(18) $N^{l}=N_{0}+d N$
(19) $\mathrm{N}_{0} \leftarrow \mathrm{~N}^{1}$
where $N_{0}$ is the initial number of animals and $N^{1}$ is the number remaining after the time step dt. The solutions of the equation are extremely stable when the dt is one day. The number of larvae are estimated after 50 days and the results are the same as previous preliminary analysis (Lett et al 1975). The final number of larvae seems to vary less than the initial number of eggs which indicates that competition among cod larvae tends to thin the population out such that carrying capacity of the environment can be met. Temperature in turn probably is modifying the food supply such that when temperature is high and more plankton is available there is less competition, thus greater survival. This same type of density dependent relationship has been noted for mackerel larvae (Lett et al MS 1975b) and is an important stabilizing force in the recruitment mechanism. Large variations in egg production and survival at this stage can be severely damped through this process. Harding and Talbot (1973) present a number of survivorship curves for plaice which indicates the same response, that is the number of surviving larvae is much more invariate than the number of eggs.

The simulated relationship between the numbers of eggs at peak spawning and larvae is shown in Fig. 12 when temperature is varied. It can be seen that at higher egg numbers the effect of temperature is more influencial in determining the numbers of larvae because of temperatures proportional influence. In addition, with a density dependent mechanism operating these larvae may be in a weakened state thus more susceptible to the influence of temperature.

## Factors effecting year-class size information

Previous attempts to derive an equation describing the formation of year-classes from larval abundance have incorporated the effects of predation of older cod on juvenile cod as they become demersal (Lett and Doubleday, 1976). However, this equation did not adequately explain the data, especially in the description of the most recent yearclasses. The conclusion that Lett and Doubleday (1976) came to was that an important variable was missing.

This most recent analysis indicates that the missing variable is possibly the impact of mackerel predation of cod larvae since mackerel enter the Gulf when cod are beginning to hatch in large numbers and remain in the same areas that cod larvae are found for the entire summer. It is known mackerel eat other fish larvae (MacKay 1976), and there is no reason to believe cod represent a special case. Mackerel have been shown to effect year-class formation of Gulf of St. Lawrence herring (Lett and Kohler 1976, Winters 1976). In fact, Lett et al. (1975) have suggested that mackerel are extremely influenced on the recruitment of any fish stock with which they co-habitat. Unfortunately, no stomach content data exists for mackerel while resident in the Gulf of St. Lawrence showing the consumption of cod larvae, however stomach content from the Scotian Shelf indicate gadoid larvae are consumed (Kulka, 1977).

The relationship between year class size, $N_{3}$, at age $3\left(\times 10^{-3}\right)$, $3+$ cod biomass (mt), $C_{D}$, and $2+$ mackerel $M_{k}$, biomass ( $m t$ ) is represented by the following equation. The cod biomass is the average when coincident year class is 0 and 1 group. Previously, it has been stated that the lag was 3 years, however it is apparent from the relationship between 2 year olds in surveys and 3 year olds from the VPA that year class size is formed by the second year (Fig. 5). $L_{R}$ is the abundance of larvae on day fifty after peak spawning as predicted by equations (13) and (16-18).

$$
\begin{align*}
N_{3}= & 4.22 \times 10^{-3} \cdot L_{R} \cdot \operatorname{EXP}\left[\left(-1.4096 \times 10^{-8} \cdot C_{B} \cdot M_{k}^{0.5}\right)+\right.  \tag{20}\\
& \left.\left(1.457 \times 10^{-11} \times C_{D} \times M_{k}^{0.5} \times L_{R}\right)+\left(2.584 \times 10^{-9} \times L_{R} \times C_{B}\right)\right]
\end{align*}
$$

The mackerel biomass $M_{k}$ is taken to the exponent 0.5 , since it was found by nonlinear regression that this exponent gave the best fit. What this means then, is the rate at which mackerel feed on cod larvae, if this is indeed the way the interaction works, is about $1 / 2$ as effective as an equivalent biomass of cod feeding juveniles.

$$
\frac{0.559}{C_{D} \times M_{k}^{0.5}} \begin{array}{lll}
L_{R} & -5.160 \times 10^{-3} & 0.087 \\
C_{D} \times M_{k}^{0.5} \times L_{R} & 1.457 \times 10^{-11} & 0.028 \\
L_{R} \times C_{D} & 2.584 \times 10^{-9} & 0.109
\end{array}
$$

The coefficient for multiple determination was 0.781 while $F$ for regression is 12.5.

Although an auto-correlated function was used to fit the data most of the variation is explained by the interaction of cod and mackerel as competitors for the feeding on larval and juvenile cod. Thus the equation fits very well (Fig. 13). The 1964 year class was not well explained, which was a good year class for cod along the Atlantic seaboard, thus information is still missing here, but a substantial proportion of the variation among year classes can be explained by this relationship. Furthermore, the equation indicates that as mackerel and/or cod decline, or that their interaction declines, year class size should improve. Only the data between 1954 and 1972 were used to fit this curve. However, if the 1973, 1974 and 1975 year classes were also used the equation would have fit much better. Surveys indicate that these year classes have been increasing in size (see juvenile surveys section), and this has happened as both cod and mackerel have declined. A first estimate indicates that the 1975 year class is one of the largest on record for this stock, when cod and mackerel predatory biomasses were at a minimum, thus the equation seems to be working. This is the only way of substantiating any of these relationships and really only time will tell if we are on the correct track.

| Year | Observed $N_{3} \times 10^{3}$ | Estimated $N_{3} \times 10^{3}$ |
| :---: | :---: | :---: |
| 1954 | 106,681 | 129,949 |
| 55 | 110,471 | 106,851 |
| 56 | 143,344 | 133,810 |
| 57 | 134,847 | 120,288 |
| 58 | 46,119 | 49,883 |
| 59 | 60,119 | 59,118 |
| 1960 | 41,739 | 51,151 |
| 61 | 61,261 | 51,589 |
| 62 | 56,163 | 60,634 |
| 63 | 61,261 | 63,933 |
| 64 | 107,042 | 75,327 |
| 1965 | 95,111 | 78,275 |
| 66 | 56,944 | 83,675 |
| 67 | 50,480 | 64,991 |
| 68 | 74,245 | 52,787 |
| 69 | 23,460 | 30,443 |
| 1970 | 45,780 | 57,786 |
| 71 | 69,137 | 41,877 |
| 72 | 42,135 | 44,931 |

The relationship between larvae and year class size is indeed unclear (Fig. 15). There is very little relationship between the two above the production of 200 larvae per $100,000 \mathrm{~m}^{3}$ of water. In fact it is hard to imagine that a relationship exists between parent stock and recruitment for cod over a wide range of stock sizes. A relationship can only be elucidated as the stock begins to decline - a similar result noted for herring (Lett and Kohler 1976). The important relationship in a so-called stock recruitment relationship is not the parent stock but the predatory stock as cod become demersal. Thus, the changes of a good year class increase as the stock declines until some critical level is reached.

## Construction of simulation model

The simulation model was initially written in APL for "debugging" and testing purposes and later rewritten in FORTRAN. The stochastic nature of the model and the many runs necessary to calculate the correct means and deviation for the different fishing strategies made the printing capabilities of APL extremely time consuming and uneconomical. However, the explanation of how the simulation was constructed will relate to the APL model because of the ease of scientific type programming in this language.

The actual model is a group of subprograms dealing with different aspects of the simulation procedure. That is to say, that one subprogram is a group of algorithms to facilitate linear interpolations, (AFGEN), sampling from normal (GAUSS) distributions and a procedure whereby a probability is put in and a deviation is retrieved (INVGAUSS). The AFGEN algorithm is particularly useful since it allows the programmer to sample from any functional relationship. The second subprogram CODO is merely a description of variables utilized throughout the model. The next subprogram COD1 initializes the cod simulation.

COD1 begins by asking for the mackerel biomass to be run in metric tons, and fishing mortalities in the winter and summer otter trawl fisheries, gillnet fishery and line fisheries. Furthermore, questions are asked concerning the length of time the simulation is to run, the number of runs and types of output expected. Matrices are set up for the AFGEN program concerning the selection of the different gear types within the fishery. Later some calculations are made concerning $Z_{1}$ size, standing biomass and growth. In addition, the number-at-age and $1000^{\prime \prime} \mathrm{s}$ are entered. The simulation is now passed onto the next subprogram COD3.

Since the initial writing of the program it has been updated so that the winter and summer fisheries can be conducted in seasonal manner. This utilized the seasonal growth information (Fig. 7) and the seasonal distribution of the fishery (Fig. 15). Thus a number of questions relevant to management of the stock could be elucidated.

COD3 is the main body of the simulation and contains the mathematical representation of the population energetic response of the southern Gulf of St. Lawrence cod stock. First the model begins to calculate the length, $L$, based on the weight, $W$, using the following equation:

I $\quad a^{L}=\left[1.0902 \times 10^{5} \mathrm{w}\right]^{0.333}$
where the growth rate at age $a$ in year $t$ is:
VIII. $t^{\Delta W_{a}}=6.6 \times t^{B S^{-0.252}} \mathrm{x}_{t^{W}}{ }^{-0.052} \times \ln t^{B S} \cdot x_{t}{ }_{a}$
and $t^{B S}$ is the summer biomass after the winter fishery in year $t$.
The $t^{\text {MGR }}$ is now used to calculate the catch of cod eggs per $100,000 \mathrm{~m}^{3}$ of water when coupled with previously mentioned spring water temperatures and $t^{\text {MSN }}$.
IX. $t^{E G G S}=5.93 x t^{M G R}{ }^{1.22} \times \operatorname{EXP}\left(1.678 T P 1-0.167 T P I^{2}\right) \times t^{M S N} \times 10^{-3}$

From this equation it is evident that there is an optimal temperature for egg survival and that temperature is indeed very important in determining final egg numbers.

It has previously been determined by Lett and Doubleday (1976)
that temperature improves the survival of cod larvae. The following equation was developed to determine the number of cod larvae, LR, after a specific period of time:
X. $\quad \Delta L R=\left(1.639 \times 10^{-2} \ell \ln \operatorname{LR} \times\left(1-1.0683 T P 2^{2}\right)-0.04854\right) \times \operatorname{LR} \times \Delta t$
where initially:
XI. $\quad \mathrm{LR} \leftarrow_{t} \mathrm{EGGS}$
therefore:

XII

$$
t_{+} \Delta t^{L R} \longleftarrow t^{L R}+\Delta L R
$$

for a particulat time step $\Delta t$.

The total time period in the simulation was 50 days and $\Delta t$ equally 1 day. $T P 2$ is the maximum summer temperature in the Gulf, normally distributed with mean 14.39 C and standard deviation 1.28 C .

Predation by a mackerel biomass $t^{M B}$ and cannabilism by a 3+ cod biomass, $t+3^{B C}$, three years later are shown to be important in conjunction with the abundance of cod larvae to be important in the recruitment of cod. The recruitment of cod is predicted at age 3 since this is the first year of sampling data. The equation
 $-2.8070 \times 10^{-3} t-3^{L R)}$
where $t^{\text {IR was placed in the first position of the numbers at age vector and }}$ had to wait 3 simulated years before being utilized in equation XIII.

Following the calculation of yearclass size the $l_{1}$ size of cod is determined by the following equation which included a spring temperature slightly higher that that used to determine the mortality of eggs.
XIV. $\quad t^{\ell}{ }_{1}=111.69 \times \mathrm{t}_{3} 0.022 \times \ln T P 3-0.300$
where TP $3\{$ TPI +0.92

After the recruitment and other biological factors are determined, the model calculates catches in the summer fishery. This fishery contains three gear types; lines (LI), gillnets (GN) and trawls (OT), which all compete with one another. Selection for each of these fisheries
are calculated using lengths to linearly interpolate in the AFGEN algorithm. The total fishing mortality is calculated as follows.

where $\partial$ is the selection and $F$ is the instaneous fishing mortality for age a. Thus the total fraction of fish caught in this fishery is (FTOT ${ }_{a} /$ FTOT $_{a}+\mathrm{MS}$ ) where MS is the natural mortality in the summer fishery. MS is equal to 0.117 since this fishery only lasts 7 months. Thus catch each of the winter fisheries is given by the catch equation.

$$
a=15
$$

XVI. $a_{a} C_{t}(O T, G N, L L)=3 \frac{N_{a} W_{a}(1-E X P(-(F T O T a+M S)) \times F(O T, G N, L L)}{\operatorname{FTOT}_{a}+M S}$

After the winter fishery is complete the model goes through an update phase. The instantaneous growth rate is calculated by rearranging equation VIII such that.
XVII. $t_{a}^{t}=6.6 \times t^{B S}{ }^{-0.252} \times t_{a}^{-0.052} \times \ln _{t} B S$

Weight is updated by
XVIII.

$$
t+1^{W} a+1 \quad t^{W} a \quad E X P t_{a}^{G}
$$

A new weight is determined from the $\ell_{1}$ length and placed on the front of the length vector and the age 16 fish are dropped from the vector. Next the numbers at age are updated by the expression,

$$
t+1^{N} a+1 \longleftarrow t^{N} a^{E X P}-(F T O T+M S)
$$

and the number of larvae are put on the front of the abundance vector. while age 16 year old fish are dropped.

At this point in the model a number of biological factors are accumulated to be subsequently printed out. The next subprogram $C O D$ is responsible for formulating the output into matrices and calculating means and standard deviations.
these lengths are used to determine a vector of ottertrawl mesh
selections da determined by the relationship in Fig. , using the
AFGEN algorithm. The catch in the winter ottertrawl fishery is
determined by the catch equation (Beverton and Holt 1957).
where $F_{\text {WOT }}$ is the instantaneous fishing mortality in the winter otter trawl fishery and $M_{w}$ is the instantaneous natural mortality during the winter fishery and is assigned a value of 0.083 since this fishery only lasts 5 months of the year (Halliday 1972). In addition natural mortality is assumed invariate with age. After the winter fishery is complete the numbers in the abundance vector are updated in accordance with the catch. The biomass before the winter fishery, or on the "conventional" January 1 birthdate is calculated by the following equation:

III


After the calculation concerning the catches and biomass in the winter otter trawl fishery the recruitment portion of the model is activated. Since environmental factors effect the survival of cod eggs, spring temperatures (May 25 th as a convention) by sampling from a normal distribution with mean 4.84 and standard deviation 0.95 . For this procedure, the algarithm GAUSS is used. In addition to temperature, the position of the maturity
ogive in relation to length and age is important. It was shown earlier that the length of first maturity was related to the growth rate in the first year. The following equations describe shifts in the maturity ogive relation to $\ell_{1}$ growth rate:
IV. $\quad t^{M L M}=\left(99.09 \times \operatorname{EXP}\left(-0.5571 \times \ln _{t^{\ell}} 1\right)\right)+13.0$
where $M L M$ is the mean length at maturity and $\ell_{I}$ is the length at the end of the first year. It was found that on average the mean length at maturity of 13 cm greater than the length at first maturity, therefore equation IV only supplies an approximation to the real situation. Since the mean length at maturity on deviation, 8 cm , are known actual maturities at age can be calculated by the relationship:
V. $t^{\text {MAT }} a^{\longleftrightarrow} \longleftarrow$ INVGAUSS $\left(t_{a}-t^{M L M}\right) \div 8$
assuming a cumulative normal distribution.

The mature stock numbers are now calculated:

and used to calculated the weighted average growth rate, $t{ }^{M G R}$


Table 1 . Number of cod samples in 4 T - 4 Vn (Jan - April) for the various fisheries. Values across the bottom are total catches (mt) and number values down the right hand side are total numbers at age, caught after the appropriate weighing factors have been applied.

| Age | Gulf 0T | Bight OT | Danish <br> Seine | Long <br> Lines | Gill <br> Nets | Catch at Age $\times 10^{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 113 | 5 | 712 | 240 | 12 | 547 |
| 4 | 847 | 225 | 2582 | 732 | 62 | 2733 |
| 5 | 1005 | 910 | 1763 | 1012 | 48 | 3134 |
| 6 | 732 | 704 | 1097 | 475 | 212 | 2266 |
| 7 | 457 | 316 | 490 | 302 | 347 | 1496 |
| 8 | 101 | 76 | 100 | 49 | 166 | 400 |
| 9 | 46 | 113 | 48 | 30 | 132 | 269 |
| 10 | 39 | 41 | 47 | 7 | 106 | 193 |
| 11 | 22 | 34 | 13 | 5 | 57 | 107 |
| 12 | 7 | 56 | 6 | 1 | 24 | 59 |
| 13 | 7 | 19 | 1 | 1 | 26 | 43 |
| 14 | 0 | 12 | 1 | 0 | 2 | 8 |
| 15 | 0 | 3 | 0 | 0 | 0 | 2 |
| $16+$ | 1 | 30 | 0 | 0 | 2 | 16 |


able
Catch removed at age.

| Age | 1950 | 1951 | 1952 | 1953 | 1954 | 1955 | 1956 | 1957 | 1958 | 1959 | 1960 | 1961 | 1962 | 1963 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 173 | 133 | 192 | 294 | 412 | 324 | 396 | 359 | 506 | 535 | 75 | 1 | 16 | 255 |
| 4 | 728 | 638 | 1034 | 2120 | 2968 | 2336 | 2612 | 2372 | 3341 | 3535 | 3967 | 3304 | 1720 | 2123 |
| 5 | 1559 | 1462 | 1915 | 5596 | 7832 | 6165 | 6727 | 6109. | 8607 | 91.07 | 8983 | 13921 | 10887 | 4352 |
| 6 | 2703 | 2113 | 3104 | 5037 | 7049 | 5549 | 6648 | 6037 | 8506 | 9000 | 12515 | 9475 | 1889 | 16021 |
| 7 | 2772 | 2127 | 3065 | 4713 | 6596 | 5191 | 6331 | 5750 | 8101 | 8571 | 7144 | 8313 | 7870 | 14742 |
| 8 | 2495 | 1874 | 2643 | 3799 | 5319 | 4186 | 5223 | 4743 | 6683 | 7071 | 1736 | 2661 | 4290 | 6390 |
| 9 | 3327 | 2365 | 3141 | 3593 | 5029 | 3959 | 5381 | 4887 | 6885 | 7286 | 795 | 777 | 1480 | 3180 |
| 10 | 2183 | 1582 | 2146 | 2680 | 3751 | 2952 | 3878 | 3522 | 4961 | 5250 | 1812 | 506 | 589 | 984 |
| 11 | 901 | 638 | 843 | 942 | 1319 | 1038 | 1424 | 1293 | 1823 | 1929 | 388 | 741 | 153 | 392 |
| 12 | 478 | 351 | 483 | 636 | 890 | 701 | 902 | 819 | 1153 | 1221 | 279 | 385 | 178 | 137 |
| 13 | 138 | 206 | 153 | 235 | 329 | 259 | 316 | 287 | 405 | 428 | 76 | 188 | 37 | 102 |
| 14 | 128 | 94 | 130 | 173 | 243 | 191 | 245 | 222 | 314 | 332 | 93 | 174 | 26 | 37 |
| 15 | 79 | 58 | 80 | 106 | 148 | 117 | 150 | 136 | 192 | 203 | 51 | 33 | 36 | 50 |


| Age | 1964 | 1965 | 1966 | 1967 | 1968 | 1969 | $1970^{\circ}$ | 1971 | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 100 | 464 | 1498 | 700 | 310 | 327 | 26 | 2 | 1541 | 378 | 1229 | 2379 | 332 | 547 |
| 4 | 970 | 5504 | 7055 | 7068 | 8140 | 4936 | 3395 | 2476 | $14294{ }^{\prime}$ | 4396 | 3170 | 9902 | 4059 | 2733 |
| 5 | 6728 | 6148 | 10689 | 5503 | 8086 | 12530 | 14972 | 7313 | 11326 | 11878 | 3862 | 6096 | 9089 | 3134 |
| 6 | - 5863 | 9292 | 4505 | 4586 | 4674 | 3571 | 11925 | 8941 | 7193 | 5982 | 9851 | 2350 | 4996 | 2266 |
| 7 | 12038 | 4481 | 3423 | 3040 | 2916 | 2516 | 4194 | 6127 | 8479 | 4492 | 3631 | 3173 | 1513 | 1496 |
| 8 | 9261 | 8524 | 1841 | 1735 | 1276 | 2136 | -1905 | -2567 | 5128 | 3455 | 2188 | 1250 | 834 | 400 |
| 9 | 2760. | 5534 | 2262 | 407 | 753 | 917 | 1444 | 1237 | 1370 | 2204 | 2081 | 1033 | 423 | 269 |
| 10 | 1133 | 1845 | 1890 | 1021 | 434 | 785 | 727 | 554 | 719 | 740 | 1186 | 738 | 220 | 193 |
| 11 | 347 | 1004 | 867 | 901 | 899 | 212 | 569 | 156 | 452 | 380 | 300 | 571 | 143 | 107 |
| 12 | 149 | 423 | 357 | 383 | 698 | 283 | 360 | 432 | 127 | 130 | 178 | 113 | 106 | 59 |
| 13 | 103 | 150 | 242 | 171 | 259 | 292 | 239 | 42 | 92 | 63 | 74 | 47 | 34 | 43 |
| 14 | 88 | 52 | 76 | 82 | 139 | 55 | 139 | 103 | 34 | 35 | 26 | 40 | 17 | 8 |
| 15 | - 24 | 124 | 42 | 23 | 65 | 21 | 30 | 144 | 72 | 14 | 4 | 5 | 11 | 2 |

Table 3. Selection at age for the weighted combination of the different gear types.

| Age | 1960 | 1961 | 1962 | 1963 | 1964 | 1965 | 1966 | 1967 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 0.619 | 0.000 | 0.022 | 0.236 | 0.330 | 0.748 | 0.572 | 0.301 |
| 4 | 0.753 | 0.678 | 0.385 | 0.343 | 0.562 | 0.696 | 0.664 | 0.722 |
| 5 | 0.891 | 0.722 | 0.593 | 0.615 | 0.696 | 0.750 | 0.846 | 0.857 |
| 6 | 0.956 | 0.859 | 0.764 | 0.801 | 0.776 | 0.810 | 0.899 | 0.871 |
| 7 | J. 989 | 0.964 | 0.909 | 0.894 | 0.894 | 0.906 | 0.962 | 0.938 |
| 8 | 0.989 | 1.000 | 0.992 | 0.969 | 0.972 | 0.943 | 0.982 | 0.952 |
| 9 | 0.956 | 0.992 | 1.000 | 1.000 | 1.000 | 0.995 | 1.000 | 0.931 |
| 10 | 0.975 | 0.872 | 0.807 | 0.939 | 0.929 | 1.000 | 0.988 | 0.977 |
| 11 | 0.754 | 0.776 | 0.336 | 0.810 | 0.740 | 0.934 | 0.908 | 1.000 |
| 12 | 0.299 | 0.457 | 0.817 | 0.603 | 0.775 | 0.769 | 0.766 | 0.993 |
| 13 | 0.247 | 0.271 | 0.527 | 0.887 | 0.337 | 0.535 | 0.544 | 0.817 |
| 14 | 0.113 | 0.167 | 0.287 | 0.611 | 0.551 | 0.789 | 0.441 | 0.885 |
| 15 | 0.598 | 0.324 | 0.092 | 0.934 | 0.287 | 0.734 | 0.394 | 0.531 |


| Age | 1968 | 1969 | 1970 | 1971 | 1972 | 2973 | 1974 | 1975 | 1976 | 1977 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 0.252 | 0.225 | 0.041 | 0.081 | 0.204 | 0.139 | 0.196 | 0.201 |  | 0.118 |
| 4 | 0.616 | 0.563 | 0.590 | 0.651 | 0.437 | 0.470 | 0.615 | 0.606 |  | 0.467 |
| 5 | 0.876 | 0.842 | 0.752 | 0.818 | 0.744 | 0.774 | 0.851 | 0.849 |  | 0.831 |
| 6 | 0.968 | 0.942 | 0.909 | 0.891 | 0.912 | 0.901 | 0.973 | 0.972 | \$ | 0.814 |
| 7 | 0.969 | 0.954 | 0.940 | 0.912 | 0.939 | 0.961 | 1.000 | 0.997 | 罢 | 0.724 |
| 8 | 0.953 | 0.988 | 0.918 | 0.932 | 1.000 | 0.995 | 0.994 | 0.995 |  | 0.831 |
| 9 | 0.957 | 0.969 | 0.941 | 0.960 | 0.964 | 1.000 | 0.930 | 0.938 | $\pm$ | 0.747 |
| 10 | 1.000 | 1.000 | 0.931 | 0.941 | 0.913 | 0.976 | 0.998 | 1.000 | '0] | 0.943 |
| 11 | . 0.999 | 0.952 | 0.958 | 0.931 | 0.779 | 0.920 | 0.880 | 0.889 | $\underset{\sim}{\text { m }}$ | 0.905 |
| 12 | 0.983 | 0.871 | 0.925 | 0.893 | 0.778 | 0.802 | 0.811 | 0.820 | ज़ | 0.953 |
| 13 | 0.941 | 0.685 | 0.841 | 1.000 | 0.779 | 0.507 | 0.652 | 0.663 | 岴 | 0.963 |
| 14 | 0.931 | 0.955 | 0.765 | 0.604 | 0.838 | 0.945 | 0.055 | 0.055 |  | 0.995 |
| 15 | 0.471 | 0.741 | 1.000 | 0.823 | 0.919 | 0.671 | 0.198 | 0.197 | 2 | 1.000 |

Table 4 . Cohort Analysis Numbers at Age $\times 10^{3} \mathrm{M}=0.2$

| AGE | 1950 | 1951 | 1952 | 1953 | 1954 | 1955 | 1956 | 1957 | 1958 | 1959 | 1960 | 1961 | 1962 | 1963 | 1964 | 1965 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 113987 | 109640 | 113532 | 108046 | 78707 | 70001 | 83924 | 106681 | 110471 | 143344 | 134847 | 46119 | 60134 | 41747 | 61261 | 52155 |
| 4 | 76132 | 93168 | 89645 | 92779 | 88195 | 64067 | 57019 | 68353 | 87018 | 89988 | 116876 | 110335 | 37758 | 49219 | 33949 | 50066 |
| 5 | 62446 | 61673 | 75703 | 72460 | 74043 | 69522 | 50340 | 44320 | 53817 | 68221 | 70478 | 92101 | 87345 | 29357 | 38376 | 26917 |
| 6 | 41633 | 49716 | 49171 | 60247 | 54262 | 53534 | 51342 | 35128 | 30758 | 36274 | 47615 | 49574 | 62809 | 61662 | 20098 | 25332 |
| 7 | 27950 | 31641 | 38792 | 37449 | 44769 | 38.488 | 38809 | 36020 | 23298 | 17486 | 21555 | 27660 | 32015 | 49715 | 35988 | 11150 |
| 8 | 17732 | 20376 | 23981 | 28987 | 26396 | 30685 | 26454 | 26046 | 24288 | 11745 | 6561 | 11184 | 15124 | 19090 | 27364 | 18572 |
| 9 | 12106 | 12260 | 14987 | 17243 | 20295 | 16799 | 21336 | 16933 | 17033 | 13838 | 3218 | 3801 | 6749 | 8501 | 9848 | 14024 |
| 10 | 6572 | 6901 | 7898 | 9428 | 10866 | 12066 | 10172 | 12599 | 9442 | 7116 | 4737 | 1915 | 2409 | 4186 | 4148 | 4661 |
| 11 | 3552 | 3405 | 4219 | 4524 | 5294 | 5502 | 7208 | 4819 | 7129 | 3241 | 1567 | 2239 | 1110 | 1440 | 2537 | 2371 |
| 12 | 1755 | 2093 | 2211 | 2691 | 2852 | 3141 | 3566 | 4613 | 2775 | 4187 | 908 | 932 | 1163 | 771 | 824 | 1763 |
| 13 | 817 | 1004 | 1396 | 1373 | 1628 | 1530 | 1937 | 2103 | 3036 | 1229 | 2323 | 491 | 415 | 791 | 507 | 540 |
| 14 | 461 | 544 | 726 | 1005 | 912 | 1035 | 1018 | 1300 | 1463 | 2119 | 619 | 1833 | 232 | 306 | 555 | 322 |
| 15 | 3400 | 261 | 360 | 477 | 666 | 527 | 675 | 612 | 864 | 913 | 1435 | 423 | 1344 | 167 | 217 | 375 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| ATE | 1900 | 1967 | 1968 | 1969 | 1970 | 1971 | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 | $\cdots$ |  |  |  |
| 3 | 61216 | 106187 | 94972 | 57488 | 53455 | 76274 | 30455 | 52562 | 60673 | 42499 | 76794 | $79630$ |  |  |  |  |
| 4 | 42281 | 48764 | 86305 | 77476 | 46771 | 43742 | 62446 | 23540 | 42692 | 48563 | 32642 | 62574 |  |  |  |  |
| 5 | 36010 | 28233 | 33529 | 63295 | 58965 | 35221 | 33573 | 38193 | 15296 | 32085 | 30800 | 23053 |  |  |  |  |
| - | 16475 | 19811 | 18136 | 20135 | 40484 | 34730 | 22220 | 17239 | 20522 | 9029 | 20753 | 16993 |  |  |  |  |
| 7 | 12332 | 9423 | 12070 | 10619 | 13254 | 22356 | 20344 | 11684 | 8701 | 7889 | 5266 | 12471 |  |  |  |  |
| 3 | 5074 | 7000 | 4956 | 7244 | 6418 | 7057 | 12759 | 8984 | 5501 | 3839 | 3588 | 2942 |  |  |  |  |
| 9 | 7493 | 2489 | 4161 | 2903 | 3998 | 3531 | 3455 | 5807 | 4230 | 2524 | 2012 | 2183 |  |  |  |  |
| 10 | 6475 | 4088 | 1669 | 2726 | 1547 | 1967 | 1772 | 1589 | 2760 | 1580 | 1132 | 1265 |  |  |  |  |
| 11 | 2147 | 3591 | 2423 | 974 | 1521. | 609 | 1109 | 800 | 631 | 1187 | 626 | 728 |  |  |  |  |
| 12 | 1033 | 973 | 2125 | 1171 | 606 | 731 | 357 | 499 | 311 | 246 | 455 | 383 |  |  |  |  |
| 13 | 1001 | 523 | 450 | 1108 | 702 | 170 | 208 | 178 | 291 | 94 | 99 | 277 |  |  |  |  |
| 14 | $300^{\circ}$ | - 50 | 273 | 134 | 643 | 359 | 102 | 87 | 89 | 172 | 34 | 50 |  |  |  |  |
| 15 | 217 | 182 | 458 | 98 | 60 | 401 | 201 | 53 | 39 | 49 | 104 | 13 |  |  |  |  |

33. 

TABLE 5. Fishing Mortality (F) from Cohort Analysis M=0.2

| AGE | 1950 | 1951 | 1952 | 1953 | 1954 | 1955 | 1956 | 1957 | 1958 | 1959 | 1960 | 1961 | 1962 | 1963 | 1964 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | . 002 | . 001 | . 002 | . 003 | . 006 | . 005 | . 005 | . 004 | . 005 | . 004 | . 001 | . 000 | . 000 | . 007 | . 002 |
| 4 | .011 | . 088 | . 013 | . 026 | . 038 | . 041 | . 052 | . 039 | . 043 | . 044 | . 038 | . 034 | . 052 | . 049 | . 032 |
| 5 | . 028 | . 027 | . 028 | . 089 | . 124 | . 103 | . 160 | . 165 | . 194 | . 160 | . 152 | . 183 | . 148 | . 179 | . 215 |
| 6 | . 074 | . 048 | . 072 | . 097 | . 155 | . 122 | . 154 | . 211 | . 365 | . 320 | . 343 | . 237 | . 034 | . 338 | . 389 |
| 7 | . 116 | . 077 | . 091 | . 150 | . 178 | . 163 | . 199 | . 194 | . 485 | .78- | . 456 | . 404 | . 317 | . 397 | . 462 |
| 8 | . 169 | .107 | . 130 | . 156 | . 252 | . 163 | . 246 | . 225 | . 363 | 1.095 | . 346 | . 305 | . 376 | . 462 | . 468 |
| 9 | . 362. | . 240 | . 263 | . 262 | . 320 | . 302 | . 327 | . 384 | . 592 | . 872 | . 319 | . 256 | . 278 | . 518 | . $548^{\prime}$ |
| 10 | . 459 | . 292 | . 357 | . 377 | . 481 | . 315 | . 541 | . 370 | . 869 | 1.394 | . 550 | . 345 | . 315 | . 301 | . 359 |
| 11 | . 329 | . 232 | . 250 | . 262 | . 322 | . 234 | . 246 | . 352 | . 332 | 1.072 | . 320 | . 455 | . 165 | . 358 | . 164 |
| 12 | . 353 | . 205 | . 276 | . 303 | . 423 | . 283 | . 328 | . 218 | . 615 | . 389 | . 415 | . 610 | . 185 | . 219 | . 223 |
| 13 | . 207 | . 124 | . 129 | .210 | . 253 | . 207 | . 199 | . 163 | . 160 | .486 | . 037 | . 550 | . 104 | . 154 | . 254 |
| 14 | . 367 | . 212 | . 221 | . 211 | . 349 | . 228 | . 309 | . 209 | . 271 | . 190 | . 182 | . 111 | . 132 | .144 | .193 |
| 15 | . 289 | . 280 | . 280 | . 280 | . 280 | . 280 | . 280 | . 280 | . 280 | . 280 | . 040 | . 090 | . 030 | . 400 | . 130 |
| AGE | 1965 | 1966 | 1967 | 1968 | 1969 | 1970 | 1971 | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 |  |  |
| 3 | . 010 | . 027 | . 007 | . 004 | . 006 | . 001 | . 000 | . 058 | . 008 | . 023 | . 064 | . 005 | . 008 |  |  |
| 4 | . 130 | . 204 | . 175 | .110 | . 073 | . 084 | . 065 | . 292 | .231 | . 086 | . 255 | . 148 | . 049 |  |  |
| 5 | . 291 | . 398 | . 243 | . 310 | . 247 | . 329 | . 261 | . 467 | . 421 | . 327 | . 236 | . 395 | . 162 |  |  |
| 6 | . 520 | . 360 | . 296 | . 335 | . 218 | . 394 | . 335 | . 443 | . 484 | . 756 | . 339 | . 309 | . 159 |  |  |
| 7 | . 587 | . 366 | . 442 | . 311 | . 304 | .430 | . 361 | . 617 | . 553 | . 618 | . 588 | . 382 | . 141 |  |  |
| 8 | . 708 | . 513 | . 320 | . 335 | . 394 | . 398 | . 514 | . 587 | . 553 | . 579 | . 446 | . 297 | . 162 |  |  |
| 9 | . 573 | . 406 | . 199 | . 223 | . 430 | . 509 | . 490 | . 577 | . 544 | . 785 | . 602 | . 265 | . 146 |  |  |
| 10 | . 575 | . 390 | . 323 | . 339 | . 383 | . 733 | .373 | . 595 | . 723 | .644 | . 726 | . 242 | . 184 |  |  |
| 11 | . 631 | . 591 | . 325 | . 528 | . 275 | . 534 | . 333 | . 599 | . 745 | . 745 | . 759 | . 291 | . 177 |  |  |
| 12 | . 308 | . 482 | . 571 | . 451 | . 311 | 1.071 | 1.061 | . 500 | . 340 | 1.002 | . 712 | . 298 | . 186 |  |  |
| 13 | . 367 | . 291 | . 449 | 1.012 | . 344 | .472 | . 319 | . 676 | . 499 | . 330 | . 812 | . 481 | . 188 |  |  |
| 14 | . 197 | . 321 | . 250 | . 829 | . 605 | . 273 | . 382 | . 465 | . 595 | . 394 | . 299 | .806 | . 194 |  |  |
| 15 | . 450 | . 240 | .150 | . 170 | .270 | . 790 | .500 | . 500 | . 350 | .120 | . 120 | . 124 | . 195 |  |  |



Fig. 1. Selection of different gear types within the $4 \mathrm{~T}-4 \mathrm{Vn}$ (January-April) cod fishery.


Fig. 2 Average fishing mortality from VPA age 3-15 versus fishing effort.

C.U.E. $2^{\text { }}$ Guif Survey Year t

Fig. 3. Relationship between the cod of $3+$ from VPA and $2+$ cod the fall before from Gulf surveys.


Fig. 4. Average catch per hour fished from research vessel survev betwapn $197 t$ and 1077 t. natah.n.


Fig. 7. Seasonal growth of cod (cumulative) based on laboratory


Fig. 8. Maturity ogives for females between 1959-74.


Fig. 9. The mean age of maturity as a function of the $1_{1}$ growth rate.


Fig. 10. Bistribution of cod eggs in the Gulf of St. Lawrence during peak spawning (May-june).


Fig. 11. The relationship between weighted mean growth rate for mature fish egg catch per mature individual. The relationship has been corrected to $5^{\circ} \mathrm{C}$.


Figure 12. Simulated relationship between the number of eggs at peak spawning and the numbers of larvae 50 days later.


Fig. 13. The relationship between observed and estimated year-class size using equation (20).


Fig. 14. Relationship between year-class size $\times 10^{7}$ and larvae for a fixed mackerel biomass and varying cod biomass.


Fig. 15. Seasonal distribution of fishery between 1960 and 1976.


Fig. 16. Relationship between catch and biomass at different levels of mackerel biomass.


Fig. 17. Relationship between time and biomass.

## APPENDIX

ainle $1 A$. Nominal catches ( mt ) for Canadian cod fishery in $4 T$ by month and gear.

|  |  |  |  |  |  | 4 TCO |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| catch | Jan | Feb | Mar | Apr | Hay | June | July | Aug | Sept | Oct | Nov | Dec | Total Catch |
| Traps | - | - | - | - | 1.7 | 10.1 | 12.2 | - | - | 4.2 | - | - | 28.1 |
| Drift Vets | - | - | - | - | 2.4 | 2.3 | 48.1 | 72.4 | 4.6 | - | - | - | 150.0 |
| Fixed cill Nets | - | - | - | 5.5 | 193.0 | 792.6 | 1163.1 | 883.3 | 520.7 | 166.4 | 68.2 | - | 3792.8 |
| tundines | - | - | - | - | 37.0 | 199.3 | 302.8 | 223.9 | 154.1 | 97.4 | 94.6 | 5.2 | 1114.3 |
| Mise. | - | - | - | - | 103.3 | 138.6 | 155.2 | 126.1 | 74.6 | 81.8 | 17.4 | - | 696.9 |
| Unspec. | - | - | - | - | 8.7 | 45.8 | 13.5 | 12.5 | 30.2 | 50.7 | 52.6 | - | 214.1 |
| Snrifap Trawl | - | - | - | - | 19.6 | 1.0 | 4.2 | 5.4 | 9.3 | 48.5 | 45.2 | - | 133.2 |
| side ot | - | - | - | 9.4 | 1614.6 | 1427.2 | 1367.4 | 1400.5 | 730.3 | 933.7 | 1392.3 | 32.7 | 8908.0 |
| Stem OT | - | - | 10.9 | 4.6 | 111.4 | 0.4 | 1.1 | 7.1 | 11.5 | 103.1 | 106.2 | 0.5 | 356.7 |
| Longlines | - | - | - | - | - | 10.1 | 78.2 | 28.5 | 15.0 | 16.5 | 32.8 | 11.1 | 192.1 |
| Purse Seine | - | - | - | - | - | 0.8 | 0.8 | - | - | - | - | - | 1.6 |
| Danish seine | - | - | - | - | 312.8 | 266.8 | 298.1 | 408.6 | 364.8 | 299.2 | 708.7 | 12.3 | 2671.3 |
| Scottish Seine | - | - | - | - | 39.0 | 31.3 | 83.0 | 35.1 | 47.2 | 13.0 | 70.8 | 14.1 | 333.5 |
| Hidwater | - | - | - | - | - | . | 1.4 | 1.5 | - | - | - | 20.1 | 23.0 |
| Par Seine | - | - | - | - | - | - | 1.6 | 0.4 | - | - | - | - | 2.0 |

Table 1B. Nominal catches (mt) for Canadian cod fishery in 4 Vn from January - April by gear.

$\triangle$

lable 2B. (comt'd) $4 T$

i.angline and

| 1970 | 957 | 447 | 2.14 | - | - | - |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71 | 1352 | 620 | 2.18 | - | - | - |
| 72 | 494 | 352 | 1.40 | - | - | - |
| 73 | 154 | 98 | 1.57 | - | -. | - |
| 74 | 39 | 31 | 1.26 | 686 | 125 | 5.49 |
| 75 | 48 | 74 | 0.65 | - | - | - |
| 76 | - | - | - | - | - | - |
| 77 | - | - | - | - | - | - |

Gillnet

Seine

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| 1970 | 962 | 337 | 2.85 | - | - | - |
| 71 | 1153 | 581 | 2.98 | - | - | - |
| 72 | 1188 | 407 | 2.92 | - | - | - |
| 73 | 890 | 408 | 2.18 | - | - | - |
| 74 | - | - | - | - | - | - |
| 75 | - | - | - | - | - |  |
| 76 | 151 | 65 | 2.32 | - | - |  |
| 77 |  |  |  | - | - | - |

Tuble $3 A$ chtch, effort and cue for canadian and loreigul vessels in oree avn.


Table 3B. (cont'd) 4 Vn


Longline and Handline


Tuote 4 . Total catines (me) and percentage catch for different gear and vessel types within months.

|  | Jan | Feb | Mar | Apr | May | June | July | Aug | Sept | Oct | Nov | Dec | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H:A, OT < SU | 35 3 | 13. | ${ }^{8} .2$ | 862 30 | $\begin{array}{r} 950 \\ 33 \end{array}$ | 745 26 | 50 2 | 30 1 | 94 3 | 54 2 |  | 54 2 | 2892 100 |
| $+\mathrm{Wa}, \mathrm{UT}>50$ | $\begin{gathered} 27393 \\ 18.4 \end{gathered}$ | $\begin{array}{r} 319+2 \\ 21.5 \end{array}$ | $\begin{gathered} 23137 \\ 15.0 \end{gathered}$ | $\begin{gathered} 21541 \\ 14.5 \end{gathered}$ | $\begin{aligned} & 15643 \\ & 10.5 \end{aligned}$ | $\begin{gathered} 9270 \\ 6.2 \end{gathered}$ | $\begin{gathered} 1700 \\ 1.1 \end{gathered}$ | $\begin{array}{r} 2112 \\ 1.4 \end{array}$ | $\begin{array}{r} 3392 \\ 2.3 \end{array}$ | ${ }_{1.5}^{2269}$ | ${ }_{1.6}^{2330}$ | $\begin{gathered} 11278 \\ 7.6 \end{gathered}$ | $\begin{array}{r} 148775 \\ 100 \end{array}$ |
| $+T, \underset{q}{ } \underset{i}{ }<50$ | 58 | 0 | 0 | ${ }^{553 .} .3$ | $\begin{array}{r} 18930 \\ 12 \end{array}$ | 30893 $19.6$ | $\begin{aligned} & 34268 \\ & 21.7 \end{aligned}$ | $\begin{array}{r} 23944 \\ 15.2 \end{array}$ | $\begin{gathered} 21191 \\ 13.4 \end{gathered}$ | $\begin{gathered} 17029 \\ 10.8 \end{gathered}$ | $\begin{aligned} & 10003 \\ & 6.3 \end{aligned}$ | ${ }^{773} .5$ | $\begin{array}{r} 157793 \\ 100 \end{array}$ |
| $+T, \underset{\substack{z \\ z}}{ }>50$ | $\begin{array}{r} 21431 \\ 12 \end{array}$ | $\begin{aligned} & 5628 \\ & 3.2 \end{aligned}$ | ${ }^{1325} .7$ | $\begin{array}{r} 17476 \\ 9.8 \end{array}$ | $\begin{array}{r} 16516 \\ 9.2 \end{array}$ | $\begin{gathered} 21213 \\ 11.9 \end{gathered}$ | $\begin{array}{r} 13512 \\ 7.6 \end{array}$ | 9388 $5.2$ | $\begin{array}{r} 7905 \\ 4.4 \end{array}$ | $\begin{gathered} 16600 \\ 9.3 \end{gathered}$ | $\begin{array}{r} 12291 \\ 6.9 \end{array}$ | $\begin{gathered} 20388 \\ 11.4 \end{gathered}$ | $\begin{array}{r} 178656 \\ 100 \end{array}$ |
| $+T$, Gillnet : | $\begin{aligned} & 5 \\ & 0 \end{aligned}$ | $\begin{aligned} & 1 \\ & 0 \end{aligned}$ | $\begin{aligned} & 4 \\ & 0 \end{aligned}$ | 58 .06 | 3970 3.92 | 15101 14.9 | $\begin{gathered} 26855 \\ 26.5 \end{gathered}$ | $\begin{aligned} & 28798 \\ & 28.5 \end{aligned}$ | $\begin{aligned} & 19516 \\ & 19.3 \end{aligned}$ | $\begin{array}{r} 5748 \\ 5.68 \end{array}$ | $\begin{aligned} & 742 \\ & .73 \end{aligned}$ | ${ }^{151} .15$ | $\begin{array}{r} 101146 \\ 100 \end{array}$ |
| $+T$, Longline | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 2 \\ & 0 \end{aligned}$ | $\begin{array}{r} 18 \\ 0 \end{array}$ | $\stackrel{134}{.12}$ | $\begin{array}{r} 7397 \\ 6.9 \end{array}$ | $\begin{array}{r} 17564 \\ 16.4 \end{array}$ | $\begin{array}{r} 27939 \\ 26.0 \end{array}$ | $\begin{array}{r} 24041 \\ 22.4 \end{array}$ | $\begin{aligned} & 14738 \\ & 13.7 \end{aligned}$ | $\begin{array}{r} 10803 \\ 10.1 \end{array}$ | $\begin{aligned} & 3960 \\ & 3.69 \end{aligned}$ | ${ }^{727} .68$ | $\begin{array}{r} 107337 \\ 100 \end{array}$ |

Table 5. $3^{+}$Biomass, 3 and $4^{+}$Numbers and Average $3^{+}$Weight

| date | $3^{+}$numbers | $3^{+}$biomass mi | average WEIGHT $\bar{W}$ | $4^{+}$numbers |
| :---: | :---: | :---: | :---: | :---: |
| 1950 | 365491 | 354429 | . 970 | 251505 |
| 1951 | 392676 | 405232 | 1.032 | 283037 |
| 1952 | 422614 | 456011 | 1.079 | 309083 |
| 1953 | 436703 | 509540 | 1.167 | 328658 |
| 1954 | 408879 | 449670 | 1.100 | 330172 |
| 1955 | 366452 | 562851 | 1.536 | 296451 |
| 1956 | 353794 | 554863 | 1.568 | 269870 |
| 1957 | 359521 | 511663 | 1.423 | 252841 |
| 1958 | 371385 | 446118 | 1.201 | 260914 |
| 1959 | 400296 | 391884 | . 979 | 256953 |
| 1960 | 412732 | 356253 | . 863 | 277886 |
| 1961 | 348601 | 353630 | 1.014 | 302483 |
| 1962 | 308600 | 434382 | 1.408 | 248467 |
| 1963 | 266945 | 263725 | . 988 | 225198 |
| 1964 | 235666 | 202722 | . 860 | 174406 |
| 1965 | 208242 | 189278 | . 909 | 156088 |
| 1966 | 192111 | 172822 | . 900 | 130898 |
| 1967 | 231893 | 166481 | . 718 | 125708 |
| 1968 | 261517 | 206075 | . 788 | 166548 |
| 1969 | 245352 | 194929 | . 794 | 187873. |
| 1970 | 228406 | 212886 | . 932 | 174955 |
| 1971 | 227120 | 216833 | . 955 | 150856 |
| 1972 | 189026 | 179494 | . 950 | 158522 |
| 1973 | 161273 | 138469 | . 859 | 108673 |
| 1974 | 161729 | 138304 | . 855 | 101112 |
| 1975 | 149755 | 128058 | . 855 | 107248 |
| 1976 | 174837 | 130720 | . 748 | 97512 |
| 1977 | 202569 | 169495 | . 836 | 122939 |

Table $\frac{6}{}$ Nominal catches by Canada for Seines $\ln 4 \mathrm{r}$ and 4 Vn In different years

|  | CANADA |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JAN | FEB | MAR | APR | MAY | JUNE | JULY | $A \cup G$ | SEPT | OCT | NOV | DEC | TOTAL |
| 4 T |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 |  |  |  |  | 15 | 42 | 27 | 34 | 38 | 24 | 32 | 17 | 227 |
| 1961 |  |  |  |  | 17 | 92 | 177 | 198 | 70 | 62 | 88 | 12 | 716 |
| 1962 |  |  |  |  | 61 | 257 | 261 | 342 | 193 | 192 | 97 | 72 | 1475 |
| 1963 | 43 |  |  |  | 101 | 314 | 391 | 309 | 200 | 148 | 55 | 60 | 1621 |
| 1964 |  |  |  |  | 99 | 416 | 648 | 321 | 165 | 169 | 90 | 81 | 1989 |
| 1965 |  |  |  |  | 264 | 654 | 636 | 385 | 281 | 135 | 146 | 172 | 2673 |
| 1966 |  |  |  | 6 | 278 | 511 | 344 | 418 | 324 | 163 | 202 | 145 | 2391 |
| 1967 |  |  |  |  | 93 | 728 | 596 | 342 | 120 | 123 | 139 | 90 | 2231 |
| 1968 |  |  |  | 1 | 61 | 410 | 267 | 95 | 40 | 20 | 40 | 48 | 982 |
| 1969 |  |  |  | 19 | 49 | 56 | 159 | 205 | 204 | 185 | 193 | 134 | 1204 |
| 1970 |  |  |  |  | 130 | 375 | 386 | 288 | 194 | 239 | 109 | 67 | 1788 |
| 1971 |  |  |  | 6 | 162 | 459 | 475 | 290 | 331 | 268 | 109 | 137 | 2237 |
| 1972 |  |  |  |  | 80 | 408 | 469 | 422 | 338 | 158 | 164 | 79 | 2118 |
| 1973 |  |  |  | * | 261 | 326 | 243 | 444 | 148 | 288 | 214 | 132 | 2056 |
| 1974 |  |  |  |  | 81 | 207 | 293 | 362 | 170 | 224 | 347 | 147 | 1731 |
| 1975 |  |  |  |  | 252 | 466 | 246 | 204 | 304 | 279 | 168 | 50 | 1969 |
| 1976 |  |  |  | 6 | 286 | 218 | 273 | 245 | 196 | 66 | 40 | 10 | 1340 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 Vn |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 1 |  |  | 3 | 35 | 19 | 5 | 4 | 3 | 2 | 5 | 5 | 82 |
| 1961 | 2 |  |  | 0 | 15 | 22 | 9 | 2 | 1 | 1 | 5 | 5 | 62 |
| 1962 | 3 |  |  | 3 | 35 | 41 | 12 | 5 | 4 | 3 | 2 | 6 | 114 |
| 1963 | 14 |  |  | 0 | 16 | 44 | 11 | 4 | 1 | 3 | 4 | 5 | 88 |
| 1964 | 0 |  |  | 2 | 5 | 27 | 5 | 1 | 2 | 6 | 2 | 21 | 71 |
| 1965 | 1 |  |  | 1 | 9 | 61 | 8 | 4 | 2 | 0 | 45 | 17 | 148 |
| 1966 | 0 |  |  | 0 | 55 | 22 | 0 | 4 | 0 | 0 | 40 | 13 | 134 |
| 1967 | $\therefore 5$ | 10 |  | 3 | 61 | 65 | 5 | 4 | 2 | 2 | 13 | 55 | 225 |
| 1968 | 0 |  | 14 | 81 | 18 | 5 | 5 | 1 | 7 | 2 | 4 | 66 | 203 |
| 1969 | 7 |  |  | 25 | 85 | 9 | 2 | 2 | 1 | 2 | 0 | 6 | 139 |
| 1970 | 0 |  |  | 4 | 39 | 22 | 9 | 3 | 2 | 3 | 0 | 5 | 87 |
| 1971 | 0 |  |  | 22 | 60 | 24 | 7 | 1 | 2 | 0 | 2 | 10 | 128 |
| 1972 | 0 |  |  | 66 | 59 | 52 | 5 | 2 | 1 | 0 | 0 | 6 | 191 |
| 1973 | 0 |  |  | 40 | 50 | 39 | 7 | 9 | 1 | 6 | 0 | 30 | 182 |
| 1974 | 3 |  |  | 7 | 90 | 14 | 7 | 0 | 0 | 0 | 4 | 23 | 148 |
| 1975 | 2 |  |  | 0 | 57 | 30 | 1 | 1 | 0 | 0 | 1 | 10 | 102 |
| 1976 | 7 |  |  | 7 | 39 | 6 | 6 | 0 | 2 | 0 | 12 | 18 | 97 |
| 1977 |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 7 Nominal catches by Canada for long and handlines in $4 T$ and $4 V n$ in different years and months.

|  | CANADA |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JAN | FEB | MAR | APR | MAY | JUNE | JULY | AUG | SEPT | OCT | NOV | OEC | TOTAL |
| 47 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 |  |  | 1 | 15 | 2200 | 4722 | 6083 | 4534 | 2268 | 930 | 730 | 90 | 21573 |
| 1961 |  | 1 | 1 | 1 | 77 | 422 | 1560 | 2535 | 931 | 1417 | 491 | 102 | 7538 |
| 1962 |  |  | 1 | 0 | 910 | 2708 | 3784 | 5413 | 2927 | 2274 | 740 | 296 | 19053 |
| 1963 |  |  | 2 | 3 | 305 | 2187 | . 4039 | 2170 | 2481 | 1608 | 252 | 21 | 13068 |
| 1964 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1965 |  | 1 | 2 | 29 | 365 | 398 | 667 | 565 | 577 | 293 | 61 | 36 | 2994 |
| 1966 |  |  |  | 0 | 17 | 38 | 78 | 533 | 371 | 28 | 74 | 1 | 1140 |
| 1967 |  |  |  | 0 | 10 | 351 | 762 | 1085 | 723 | 467 | 160 | 27 | 3585 |
| 1968 |  |  |  | 4 | 69 | 258 | 1026 | 668 | 543 | 367 | 172 | 20 | 3127 |
| 1969 |  |  |  | 54 | 253 | 1490 | 2939 | 1970 | 729 | 545. | 200 | 29 | 8209 |
| 1970 |  |  |  | 15 | 581 | 1828 | 2597 | 1502 | 931 | $643^{\circ}$ | 223 | 45 | 8365 |
| 1971 |  |  |  | 10 | 834 | 1354 | 1783 | 1069 | 823 | 578 | 273 | 14 | 6738 |
| 1972 |  |  |  | 0 | 173 | 474 | 658 | 703 | 370 | 385 | 218 | 26 | 3007 |
| 1973 |  |  |  | 3 | 247 | 270 | 511 | 441 | 431 | 474 | 120 | 14 | 2511 |
| 1974 |  |  |  | 0 | 120 | 345 | 374 | 305 | 116 | 133 | 117 | 3 | 1513 |
| 1975 |  |  |  | 0 | 1171 | 562 | 696 | 254 | 324 | 541 | 113 | 3 | 3664 |
| 1976 |  |  |  | 0 | 63 | 157 | 382 | 290 | 193 | 118 | 12 | 0 | 1215 |


|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1960 | 615 | 663 | 113 | 216 | 235 | 343 | 510 | 388 | 233 | 151 | 183 | 230 | 3880 |
| 1961 | 253 | 5 |  | 7 | 19 | 43 | 666 | 341 | 619 | 192 | 217 | 45 | 2407 |
| 1962 | 214 | 75 |  | 32 | 11 | 82 | 788 | 454 | 507 | 387 | 405 | 516 | 3471 |
| 1963 | 656 | 42 |  | 14 | 139 | 386 | 937 | 820 | 453 | 290 | 327 | 199 | 4263 |
| 1964 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1965 | 188 | 0 |  | 7 | 172 | 169 | 531 | 428 | 690 | 284 | 805 | 719 | 3993 |
| 1966 | 73 | 56 |  | 33 | 254 | 320 | 405 | 396 | 394 | 366 | 991 | 769 | 4057 3886 |
| 1967 | 286 | 66 |  | 14 | 274 | 247 | 719 | 566 | 343 | 315 | 527 | 529 | 3886 |
| 1968 | 38 | 9 | 1 | 96 | 513 | 291 | 578 | 327 | 410 | 288 | 427 | 581 | 3559 |
| 1969 | 75 | 19 | 42 | 175 | 333 | 519 | 548 | 438 | 595 | 365 | 823 | 527 | 4459 |
| 1970 | 101 | 38 | 1 | 167 | 476 | 482 | 500 | 406 | 470 | 606 | 463 | 319 | 4029 |
| 1971 | 28 | 0 | 4 | 212 | 517 | 365 | 437 | 763 | 811 | 754 | 219 | 399 | 4509 |
| 1972 | 18 | 0 |  | 70 | 447 | 398 | 284 | 485 | 378 | 511 | 471 | 211 | 3273 |
| 1973 | 0 | 0 | 3 | 33 | 371 | 385 | 242 | 292 | 271 | 312 | 283 | 230 | 2422 |
| 1974 | 9 | 14 | 3 | 32 | 284 | 145 | 243 | 183 | 261 | 265 | 295 | 123 | 1857 |
| 1975 | 2 | 0 |  | 0 | 91 | 87 | 186 | 206 | 183 | 187 | 73 | 36 | 1051 |
| 1976 | 0 | 0 |  | 9 | 90 | 61 | 173 | 163 | 169 | 144 | 101 | 29 | 939 |

Table 8 Nominal catches by Canada for Gillnets in $4 T$ and $4 V n$ in different years and months.

CANADA
JAN FEB MAR APR MAY JUNE JULY AUG SEPT OCT NOV DEC TOTAL

| $\begin{array}{r} 4 \pi \\ 1960 \end{array}$ |  |  |  |  | 0 | 0 | 2 | 0 | 2 | 0 | 0 | 0 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1961 |  |  |  |  | 0 | 6 | 66 | 30 | 53 | 15 | 1 | 0 | 171 |
| 1962 |  |  |  |  | 18 | 103 | 246 | 266 | 398 | 105 | 8 | 2 | 1146 |
| 1963 |  |  |  |  | 7 | 342 | 1115 | 693 | 218 | 18 | 3 | 0 | 2396 |
| 1964 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1965 |  |  |  | 5 | 26 | 497 | 1238 | 997 | 646 | 130 | 31 | 1 | 3571 |
| 1966 |  |  |  | 0 | 86 | 1792 | 2108 | 2697 | 2330 | 248 | 104 | 49 | 9414 |
| 1967 |  |  |  | 0 | 85 | 1522 | 2703 | 3479 | 1735 | 378 | 38 | 2 | 9942 |
| 1968 |  |  |  | 0 | 616 | 1421 | 3442 | 3745 | 3021 | 649 | 39 | 0 | 12933 |
| 1969 |  |  |  | 10 | 315 | 1327 | 2692 | 2878 | 1655 | 554 | 128 | 19 | 9578 |
| 1970 |  |  |  | 5 | 451 | 730 | 2573 | 2912 | 1778 | 1188 | 92 | 60 | 9789 |
| 1971 |  |  |  | 2 | 354 | 1766 | 2192 | 2731 | 1937 | 383 | 11 | 0 | 9376 |
| 1972 | 0 |  | 2 | 20 | 487 | 1002 | 2030 | 2143 | 1424 | 694 | 51 | 9 | 7862 |
| 1973 | 4 |  | 1 | 0 | 88 | 1492 | 2015 | 2461 | 1490 | 541 | 39 | 0 | 8131 |
| 1974 |  |  |  | 0 | 65 | 905 | 2083 | 1480 | 1107 | 315 | 102 | 0 | 6057 |
| 1975 |  |  |  | 6 | 1089 | 1089 | 1336 | 1439 | 1064 | 235 | 60 | 9 | 6327 |
| 1976 |  |  |  | 10 | 283 | 1107 | 1214 | 847 | 658 | 295 | 35 | 0 | 4449 |
| 4 Vn |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1961 | 0 | 0 | 0 | 0 | 0 | 0 | 4 | 5 | 7 | 0 | 0 | 0 | 16 |
| 1962 | 0 | 0 | 0 | 0 | 0 | 0 | 3 | 2 | 27 | 1 | 0 | 1 | 34 |
| 1963 | 0 | 0 | 0 | 0 | 3 | 4 | 15 | 53 | 23 | 12 | 0 | 0 | 110 |
| 1964 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1965 | 0 | 0 | 0 | 0 | 0 | 0 | 33 | 49 | 28 | 0 | 0 | 0 | 110 |
| 1966 | 0 | 0 | 0 | 0 | 0 | 5 | 47 | 30 | 19 | 4 | 0 | 0 | 105 |
| 1967 | 0 | 0 | 0 | 0 | 0 | 0 | 12 | 71 | 46 | 4 | 6 | 0 | 139 |
| 1968 | 0 | 0 | 0 | 0 | 0 | 15 | 32 | 28 | 23 | 12 | 0 | 0 | 110 |
| 1969 | 0 | 0 | 0 | 0 | 0 | 0 | 22 | 43 | 35 | 12 | 3 | 0 | 115 |
| 1970 | 0 | 0 | 0 | 6 | 0 | 1 | 12 | . 37 | 20 | 5 | 0 | 0 | 81 |
| 1971 | 0 | 0 | 0 | 0 | 0 | 4 | 1 | 14 | 18 | 4 | 0 | 0 | 41 |
| 1972 | 0 | 0 | 0 | 0 | 2 | 0 | 1 | 39 | 67 | 106 | 33 | 0 | 248 |
| 1973 | 0 | 0 | 0 | 0 | 0 | 3 | 139 | 180 | 147 | 86 | 67 | 27 | 649 |
| 1974 | 0 | 0 | 0 | 0 | 0 | 132 | 120 | 88 | 147 | 156 | 61 | 10 | 714 |
| 1975 | 0 | 0 | 0 | 0 | 99 | 58 | 99 | . 199 | 109 | 37 | 3 | 0 | 604 |
| 1976 | 0 | 0 | 0 | 0 | 9 | 19 | 48 | 118 | 57 | 53 | 10 | 0 | 314 |

Table 9 . Catches by Canadian vessels in 47 and 4 Va by unthe and tornage clabs.
$>50$ TONS (VESSEL)

|  | Jan | feb | mar | APR | May | June | july | alig | sepr | OCT | nov | DEC | TOTAL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 T |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 340 | 18 | 6 | 62 | 624 | 569 | 673 | 408 | 374 | 392 | 532 | 218 | 4216 |
| 1961 | 859 | 0 | 0 | 224 | 698 | 1247 | 690 | 718 | 591 | 408 | 454 | 149 | 6038 |
| 1962 | 30 | 0 | 0 | 210 | 1702 | 1225 | 1329 | 865 | 1115 | 1253 | 511 | 339 | 8579 |
| 1963 | 884 | 100 | 0 | 235 | 3429 | 2183 | 1956 | 1824 | 1177 | 696 | 451 | 149 | 13084 |
| 1964 | 141 | 0 | 0 | 355 | 2120 | 1796 | 2360 | 1268 | 843 | 461 | 440 | 466 | 10270 |
| 1965 | 1429 | 864 | 0 | 1531 | 3847 | 2211 | 929 | 531 | 503 | 591 | 960 | 2442 | 15838 |
| 1966 | 1121 | 149 | 94 | 1448 | 1391 | 922 | 213 | 381 | 301 | 530 | 1348 | 1401 | 9299 |
| 1967 | 1684 | 205 | 0 | 145 | 2026 | 1403 | 435 | 125 | 191 | 349 | 563 | 1290 | 8416 |
| 1968 | 1088 | 0 | 0 | 2429 | 3025 | 862 | 683 | 536 | 337 | 654 | 564 | 1719 | 11897 |
| 1969 | 1795 | 830 | 1083 | 2242 | 1840 | 897 | 850 | 510 | 387 | 435 | 1021 | 1611 | 13501 |
| 1970 | 3115 | 1637 | 99 | 1122 | 2166 | 1019 | 795 | 465 | 335 | 493 | 747 | 953 | 12946 |
| 1971 | 1740 | 1228 | 30 | 2358 | 2447 | 1180 | 862 | 379 | 414 | 382 | 713 | 1346 | 13079 |
| 1972 | 3928 | 318 | 0 | 1936 | 5938 | 3413 | 501 | 267 | 227 | 227 | 768 | 2056 | 19579 |
| 1973 | 430 | 0 | 0 | 1067 | 1346 | 885 | 372 | 252 | 125 | 228 | 698 | 1609 | 7012 |
| 1974 | 882 | 0 | 0 | 536 | 1.298 | 370 | 103 | 94 | 154 | 328 | 688 | 2382 | 6835 |
| 1976 | 68 | 1 | 0 | 253 | 2790 | 467 | 181 | 194 | 165 | 530 | 782 | 2205 | 7636 |
| 1976 | 1890 | 279 | 10 | 1301 | 2014 | 446 | 522 | 468 | 592 | 291 | 124 | 33 | 7970 |
|  | 6.5 | 0 | 3.3 | 22.3 | 683 | 118 | 59.7 | 103 | 72.3 | 446.5 | 926.8 | 19.8 | 2461 |
| 4 Vn |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 162 | 420 | 49 | 242 | 650 | 507 | 4 | 10 | 0 | 1 | 31 | 7 | 2083 |
| 1961 | 202 | 58 | 0 | 51 | 391 | 283 | 31 | 9 | , | 126 | 22 | 38 | 1211 |
| 1962 | 35 | 696 | 121 | 368 | 457 | 1669 | 242 | 46 | , | 236 | 17 | 56 | 3945 |
| 1963 | 955 | 536 | 512 | 820 | 1622 | 689 | 23 | 10 | 12 | 109 | 78 | 113 | 5479 |
| 1964 | 1146 | 1430 | 4877 | 1527 | 2538 | 936 | 184 | 195 | 305 | 2 | 83 | 420 | 11173 |
| 1965 | 689 | 4415 | 2005 | 3589 | 1508 | 1263 | 124 | 21 | 93 | 66 | 142 | 257 | 14172 |
| 1966 | 1906 | 2708 | 2221 | 3420 | 748 | 810 | 243 | 202 | 38 | 75 | 50 | 285 | 12706 |
| 1967 | 685 | 737 | 416 | 0 | 166 | 254 | 131 | 265 | 216 | 171 | 104 | 527 | 3672 |
| 1968 | 2308 | 1699 | 476 | 1573 | 655 | 397 | 41 | 0 | 22 | 0 | 63 | 663 | 7897 |
| 1969 | 1149 | 1871 | 1244 | 531 | 1296 | 499 | 55 | 112 | 899 | 140 | 110 | 329 | 8235 |
| 1970 | 886 | 2196 | 1017 | 321 | 585 | 705 | 477 | 394 | 51 | 899 | 73 | 493 | 8097 |
| 1971 | 806 | 2201 | 897 | 2779 | 403 | 376 | 28 | 475 | 986 | 112 | 113 | 637 | 9813 |
| 1972 | 2705 | 1501 | 499 | 2018 | 1227 | 106 | 19 | 57 | 627 | 36 | 188 | 235 | 9218 |
| 1973 | 4517 | 969 | 93 | 2052 | 1077 | 135 | 50 | 8 | 8 | 90 | 93 | 302 | 9394 |
| 1974 | 2101 | 4122 | 2588 | 994 | 1072 | 295 | 27 | 34 | 7 | 46 | 26 | 371 | 11683 |
| 1975 | 2190 | 2320 | 1962 | 402 | 504 | 173 | 8 | 7 | 84 | 23 | 59 | 524 | 8266 |
| 1976 | 4187 | 3265 | 3480 | 786 | 322 | 136 | 2 | 1 | 33 | 87 | 511 | 3036 | 15847 |
| 1977 | 764 | 797 | 610 | 68 | 422 | 37 | 11 | 266 | 9.2 | 50.4 | 566.7 | 2685 | 5884 |

Table 10. Catches by Canadian vessels < 50 tons in $4 T$ and $4 V n$ by month.

|  | O.T. < 50 tons (vessel) |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JAN | feb | March | APRIL | may | June | July | aug | SEPT | oct | nov | DEC | total |
| 1960 | 16 | 0 | 0 | 154 | 1302 | 1443 | 1772 | 1448 | 1325 | 1248 | 999 | 97 | 9804 |
| 61 | 13 | 0 | 0 | 0 | 815 | 2998 | 2459 | 2145 | 2081 | 1470 | 1218 | 82 | 13281 |
| 62 | 0 | 0 | 0 | 0 | 1668 | 3685 | 4014 | 2479 | 2975 | 2745 | 841 | 277 | 18684 |
| 63 | 0 | 0 | 0 | 0 | 1807 | 3833 | 4327 | 3637 | 2551 | 1371 | 780 | 54 | 18360 |
| 64 | 0 | 0 | 0 | 0 | 1642 | 2676 | 4296 | 2850 | 2071 | 1323 | 645 | 16 | 15519 |
| 65 | 0 | 0 | 0 | 99 | 3686 | 3123 | 3189 | 1574 | 1766 | 1044 | 664 | 42 | 15187 |
| 66 | 0 | 0 | 0 | 353 | 1221 | 2044 | 1090 | 1524 | 1532 | 1221 | 866 | 72 | 9923 |
| 67 | 0 | 0 | 0 | 0 | 859 | 1929 | 1994 | 851 | 718 | 640 | 523 | 22 | 7536 |
| 68 | 0 | 0 | 0 | 24 | 689 | 1290 | 1406 | 1296 | 1162 | 1117 | 590 | 2 | 7576 |
| 69 | 0 | 0 | 0 | 56 | 378 | 1457 | 1766 | 1307 | 901 | 647 | 519 | 17 | 7048 |
| 70 | 0 | 0 | 0 | 21 | 723 | 1565 | 2377 | 1284 | 978 | 1039 | 503 | 44 | 8534 |
| 71 | 29 | 0 | 0 | 0 | 731 | 1283 | 1917 | 897 | 663 | 887 | 468 | 6 | 6881 |
| 72 | 0 | 0 | 0 | 0 | 1047 | 1512 | 894 | 689 | 621 | 477 | 402 | 33 | 5673 |
| 73 | 0 | 0 | 0 | 0 | 297 | 709 | 974 | 626 | 526 | 593 | 448 | 0 | 4173 |
| 74 | 0 | 0 | 0 | 0 | 309 | 381 | 372 | 321 | 398 | 459 | 318 | 4 | 2562 |
| 75 | 0 | 0 | 0 | 0 | 1104 | 620 | 697 | 669 | 458 | 493 | 185 | 5 | 4231 |
| 76 | 0 | 0 | 0 | 0 | 596 | 293 | 678 | 329 | 408 | 194 | 15 | 0 | 2513 |
| 77 | 0 | 0 | 0 | 0 | 56.3 | 52.2 | 46 | 18.1 | 55.6 | 60.6 | 19.2 | 0 | 308 |
| 4 Vn |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 25 | 13 | 0 | 140 | 84 | 76 | 3 | 0 | 3 | 1 | 6 | 20 | 371 |
| 61 | 47 | 0 | 0 | 0 | 97 | 73 | 1 | 0 | 1 | 0 | 6 | 6 | 227 |
| 62 | 0 | 0 | 0 | 33 | 212 | 63 | 4 | 0 | 0 | 4 | 0 | 5 | 321 |
| 63 | 13 | 0 | 5 | 24 | 238 | 74 | 0 | 0 | 0 | 0 | 11 | 0 | 365 |
| 64 | 0 | 0 | 0 | 0 | 68 | 0 | 0 | 0 | 55 | 0 | 0 | 0 |  |
| 65 | 0 | 0 | - | 0 | 86 | 159 | 8 | - 5 | 0 | 0 | 0 | 5 | 263 |
| 66 | 0 | 0 | 0 | 21 | 134 | 261 | 12 | 22 | 0 | 2 | 4 | 0 | 456 |
| 67 | 0 | 0 | 3 | 641 | 0 | 8 | 1 | 0 | 0 | 0 | 0 | 0 | 653 |
| 68 | 0 | 0 | 0 | 0 | 0 | 13 | 0 | 0 | 0 | 42 | 0 | 0 | 55 |
| 69 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 70 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 71 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 72 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 73 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |  | 0 | 0 | 2 |
| 74 | 0 | 0 | 0 | 0 | 13 | 10 | 7 | 1 | 4 | 1 | 0 | 5 | 31 |
| 75 | 0 | 0 | 0 | 0 | 1 | 2 | 13 | 2 | 0 | 2 | 0 | 0 | 20 |
| 76 | 0 | 0 | 0 | 3 | 3 | 3 | 0 | 0 | 30 | 1 | 0 | 4 | 44 |
| 77 | 0 | 0 | 0 | 0 | 14.4 | 4.6 |  | 0 | 0 | 0 | 0 | 8.7 | 28.9 |

Table 11. Catches by foreign vessels 250 tons in 41 and $4 V n$ by month.
> TONS (VESSEL)

|  | JAN | FEB | MAR | APR | MAY | JUNE | JULY | AUG | SEPT | OCT | NOV | DEC | TORAL |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 4 4T |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1960 | 0 | 348 | 1537 | 3006 | 130 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 5021 |
| 1961 | 0 | 79 | 69 | 8067 | 36 | 0 | 0 | 0 | 0 | 0 | 4 | 0 | 8255 |
| 1962 | 0 | 418 | 108 | 111 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 637 |
| 1963 | 141 | 68 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 209 |
| 1964 | 0 | 0 | 130 | 0 | 290 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 422 |
| 1965 | 23 | 0 | 573 | 297 | 75 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1966 | 0 | 12 | 997 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1009 |
| 1967 | 69 | 58 | 757 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 884 |
| 1968 | 3 | 0 | 0 | 116 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 119 |
| 1969 | 2 | 135 | 72 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 209 |
| 1970 | 0 | 0 | 498 | 275 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 773 |
| 1971 | 0 | 0 | 25 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 25 |
| 1972 | 30 | 249 | 95 | 884 | 51 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1309 |
| 1973 | 446 | 0 | 0 | 256 | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 5 | 711 |
| 1974 | 7432 | 6 | 0 | 1100 | 106 | 0 | 0 | 0 | 0 | 0 | 0 | 42 | 8686 |
| 1975 | 903 | 1413 | 67 | 1264 | 95 | 1 | 8 | 0 | 0 | 0 | 31 | 509 | 4283 |
| 1976 | 984 | 0 | 0 | 118 | 2 | 0 | 0 | 0 | 0 | 0 | 247 | 314 | 1665 |
| 1977 |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| $4 V n$ |  |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1960 | 35 | 2439 | 12639 | 5532 | 18 | 2 | 0 | 18 | 1 | 1 | 0 |
| 1961 | 0 | 1127 | 5200 | 6867 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1962 | 0 | 1504 | 875 | 1243 | 855 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1963 | 207 | 8254 | 6227 | 1017 | 18 | 0 | 0 | 9 | 0 | 4 | 0 |
| 1964 | 690 | 6887 | 1580 | 495 | 707 | 0 | 0 | 0 | 0 | 61 | 3 |
| 1965 | 565 | 964 | 1153 | 1799 | 0 | 2045 | 167 | 168 | 18 | 216 | 32 |
| 1966 | 761 | 574 | 2168 | 502 | 60 | 257 | 57 | 159 | 202 | 18 | 0 |
| 1967 | 223 | 91 | 946 | 1923 | 0 | 0 | 0 | 14 | 0 | 1 | 0 |
| 1968 | 0 | 168 | 871 | 27 | 13 | 0 | 0 | 0 | 0 | 1 | 0 |
| 1969 | 0 | 0 | 704 | 0 | 0 | 0 | 129 | 0 | 0 | 0 | 0 |
| 1970 | 0 | 603 | 7264 | 3682 | 0 | 0 | 0 | 0 | 0 | 203 | 19 |
| 1971 | 54 | 835 | 2481 | 1281 | 0 | 0 | 0 | 0 | 1851 | 85 | 58 |
| 1972 | 1846 | 5273 | 4711 | 944 | 3 | 0 | 0 | 0 | 805 | 342 | 0 |
| 1973 | 814 | 4058 | 6873 | 118 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1974 | 2290 | 4280 | 19 | 85 | 0 | 0 | 61 | 0 | 0 | 14 | 0 |
| 1975 | 1442 | 2050 | 813 | 222 | 0 | 83 | 118 | 104 | 55 | 0 | 0 |
| 1976 | 1949 | 514 | 225 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1977 |  |  |  |  |  |  |  |  |  |  |  |

20686
13196
12397
15736
10359
7127
4758
3198
1083
904
11771
6645
13988
11936
7249
4887
2899


HO WINTER FISHERY

OPTIMAL BIOMASS - OBTAINED IN 1980


SUMMER TO WINTER OTTER TRAWL EFFORT APPROXIMATELY . 60 to . 40

## OPTIMAL BIOMASS OBTAINED IN 1980



SUMMER TO WINTER OTTER TRAWL EFFORT APPROXIMATELY . 80 to .20.


NO WINTER FISHERY

OPTIMAL BIOMASS OBTAINED IN 1985


SUMMER TO WINTER OTTER TRAWL CATCHES 40 to $60 \%$.

## OPTIMAL BIOMASS OBTAINED IN 1985




Fig. 5. Relationship between the catch of 2-year-olds in the Gulf surveys and the year-class size at age from virtual population analysis.


Fig. 6. Relationship among instantaneous growth rate, biomass and weight showing density-dependent biomass
growth.

